

# **The Bonded-Particle Model as a Tool for Rock Mechanics Research and Application**

David Potyondy

Virtual seminar for University of Twente (Enschede, Netherlands)

Multiscale Mechanics Research Group

May 6, 2021

# Preamble

- We provide an overview of Bonded-Particle Modeling, and suggest avenues for further research by summarizing & expanding on the contents of:

Potyondy, D.O. (2015) “The Bonded-Particle Model as a Tool for Rock Mechanics Research and Application: Current Trends and Future Directions,” *Geosystem Engineering*, **18**(1), 1–28.

Potyondy, D.O, and P.A. Cundall (2004) “A Bonded-Particle Model for Rock,” *Int. J. Rock Mech. & Min. Sci.*, **41**(8), 1329–1364.

- You need not be a rock-mechanics practitioner to understand this talk. So, let’s get started. . .

# Overview

- Bonded-Particle Modeling
  - Basic idea & essential features
- Microstructural Physics of intact rock
  - Micromechanical processes that control brittle fracture
  - Nature of pore space: compact or porous
  - Two complimentary idealizations of rock (BPM & LEFM)

# Overview

- Bonded-Particle Modeling Methodology
  - PFC model (distinct-element model of *synthetic material*: rigid grains that interact at contacts, vast microstructural space)
  - BPM (*bonded materials* & interface)
  - Microstructural models provided by BPM

# Overview

- Bonded-Particle Modeling Methodology
  - PFC model (distinct-element model of *synthetic material*: rigid grains that interact at contacts, vast microstructural space)
  - BPM (*bonded materials* & interface)
  - Microstructural models provided by BPM
- Examples
  - Ceramic bead and undercut cemented backfill
  - Two intact BPMs that match both uniaxial & tensile strength of compact rock
  - Embed BPM in larger continuum model
  - Sandstone perforation damage
- Conclusions & Future Directions

Poem: “What’s In My Journal” by William Stafford

*Clues that lead nowhere,  
that never connected anyway.*

*Deliberate obfuscation,* The action of making something obscure,  
unclear or unintelligible.  
*the kind that takes genius.*

This talk: “What’s In My Lecture” by David Potyondy

*Clues that spawn understanding,  
arrived at by modeling.*

*Deliberate simplification,  
the kind that gives clarity.*

There is a need for simplification in rock-mechanics modeling.

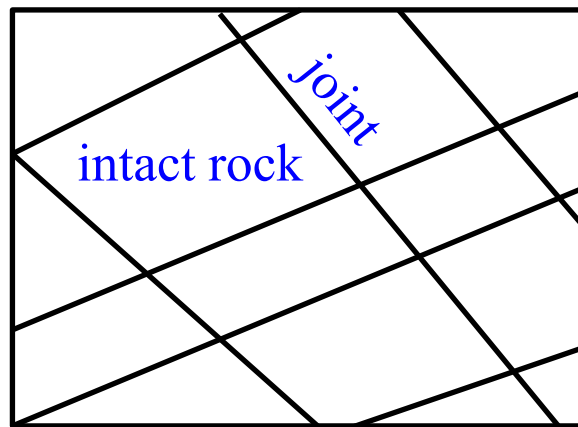
*We build models because the real world is too complex for our understanding; it does not help if we build models that are also too complex.*

*The art of modeling lies in determining what aspects of the geology are essential for the model.*

Starfield & Cundall (1988)

# Basic Idea

Rock Mass

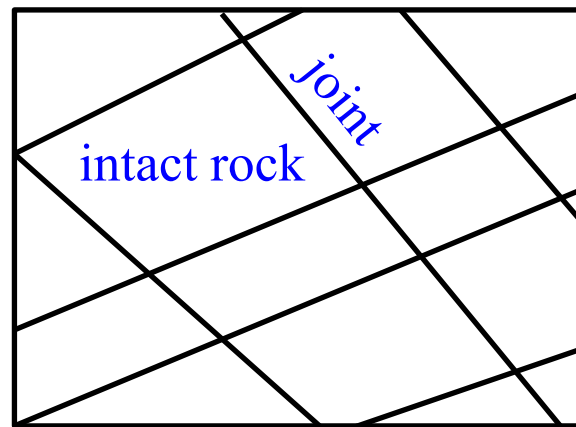


Mechanical behavior arises from interactions:

- microstructure (grain scale) of **intact rock**
- orientations & properties of **joints**

# Basic Idea

Rock Mass



*emergent phenomena*

Mechanical behavior arises from interactions:

- microstructure (grain scale) of **intact rock** → fracture & flow
- orientations & properties of **joints** → rupture & sliding

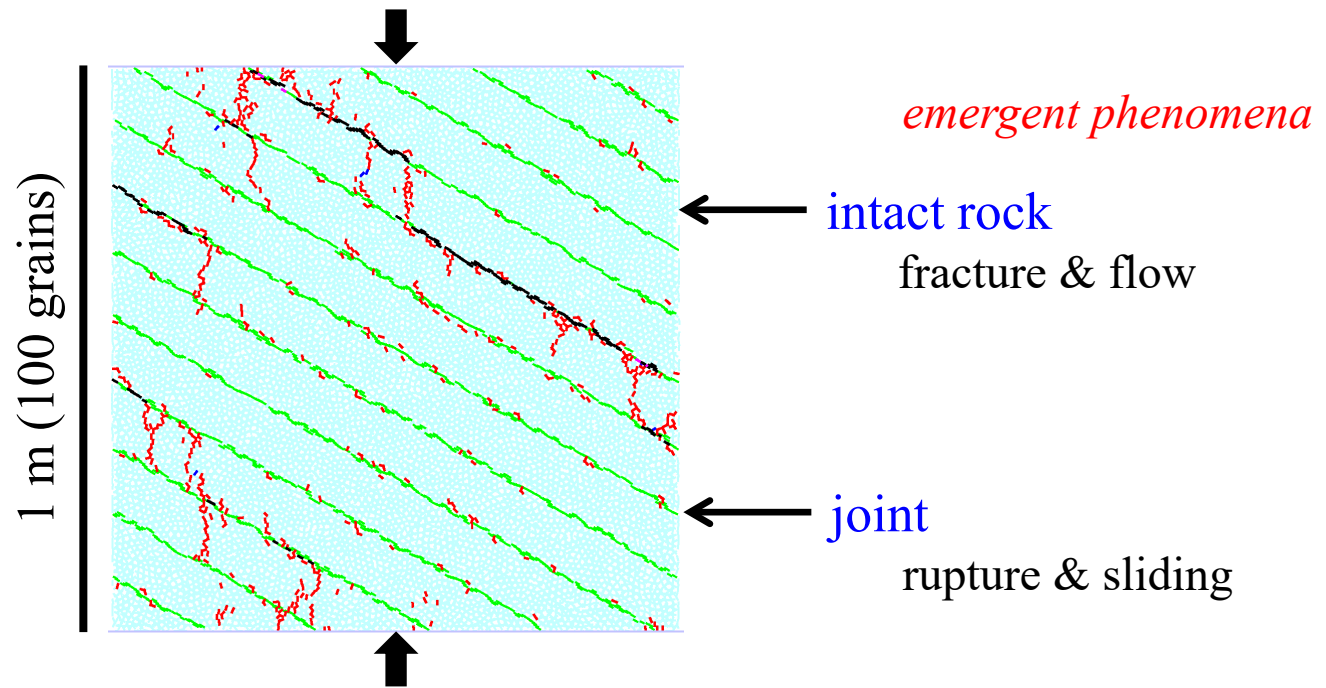
Bonded-Particle Models mimic **intact rock** & **joints**

Closer match to microstructural & structural features →  
Closer match to macroscopic behavior

# Essential Features of a BPM

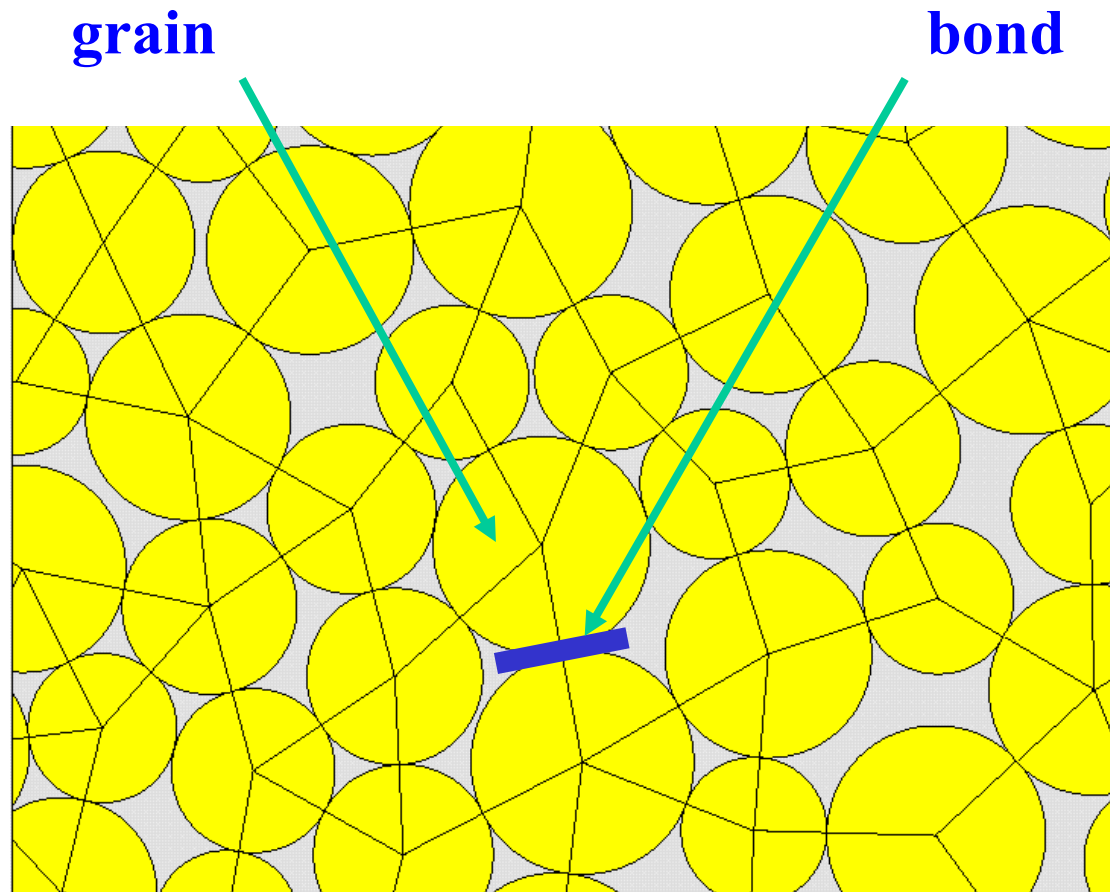
BPM consists of a base material (*intact rock*) to which larger-scale *joints* can be added.

- base material : bonded rigid grains
- joints : interfaces



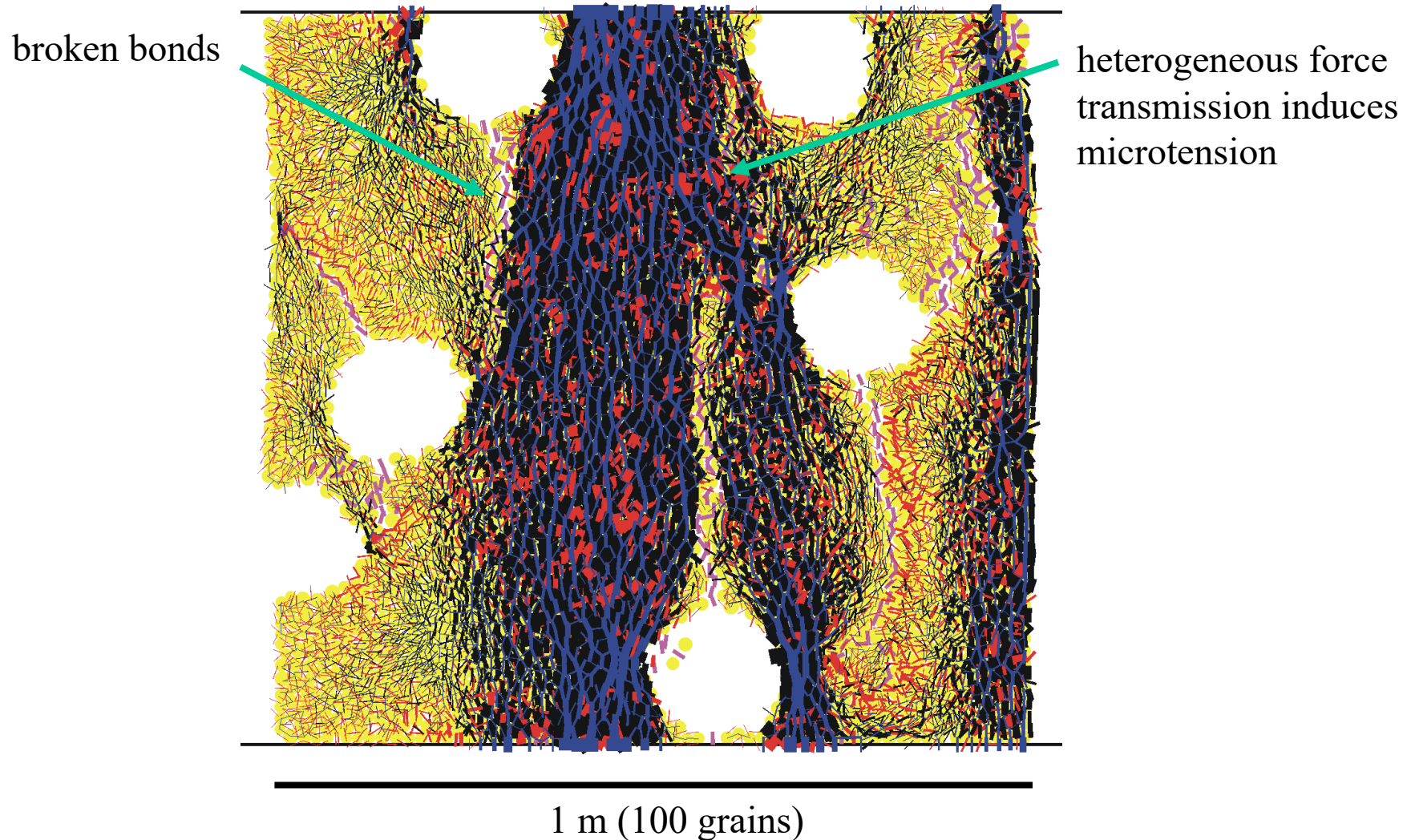
Damage consists of bond breakages.

# Essential Features of a BPM



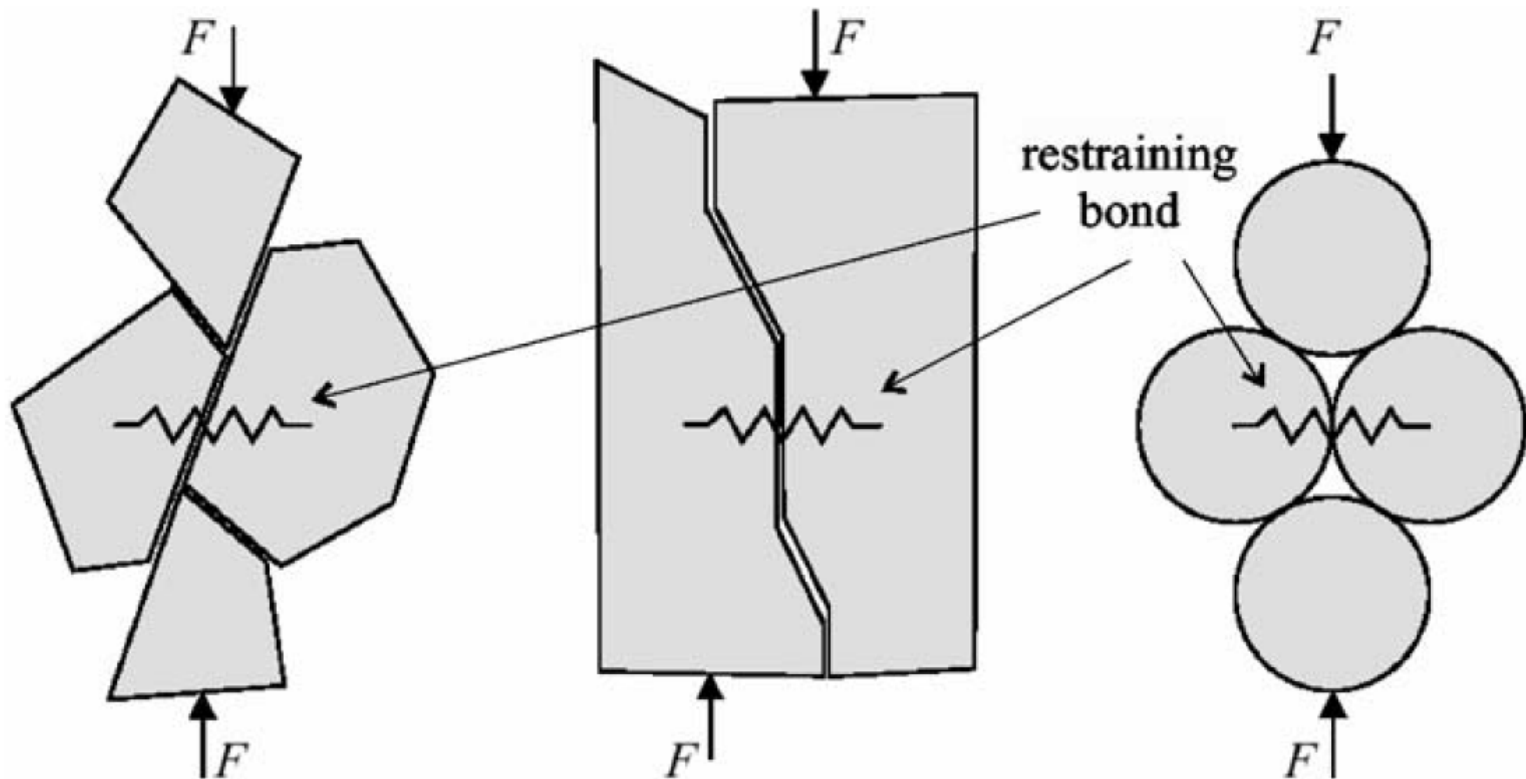
Damage consists of bond breakages.

# Essential Features of a BPM



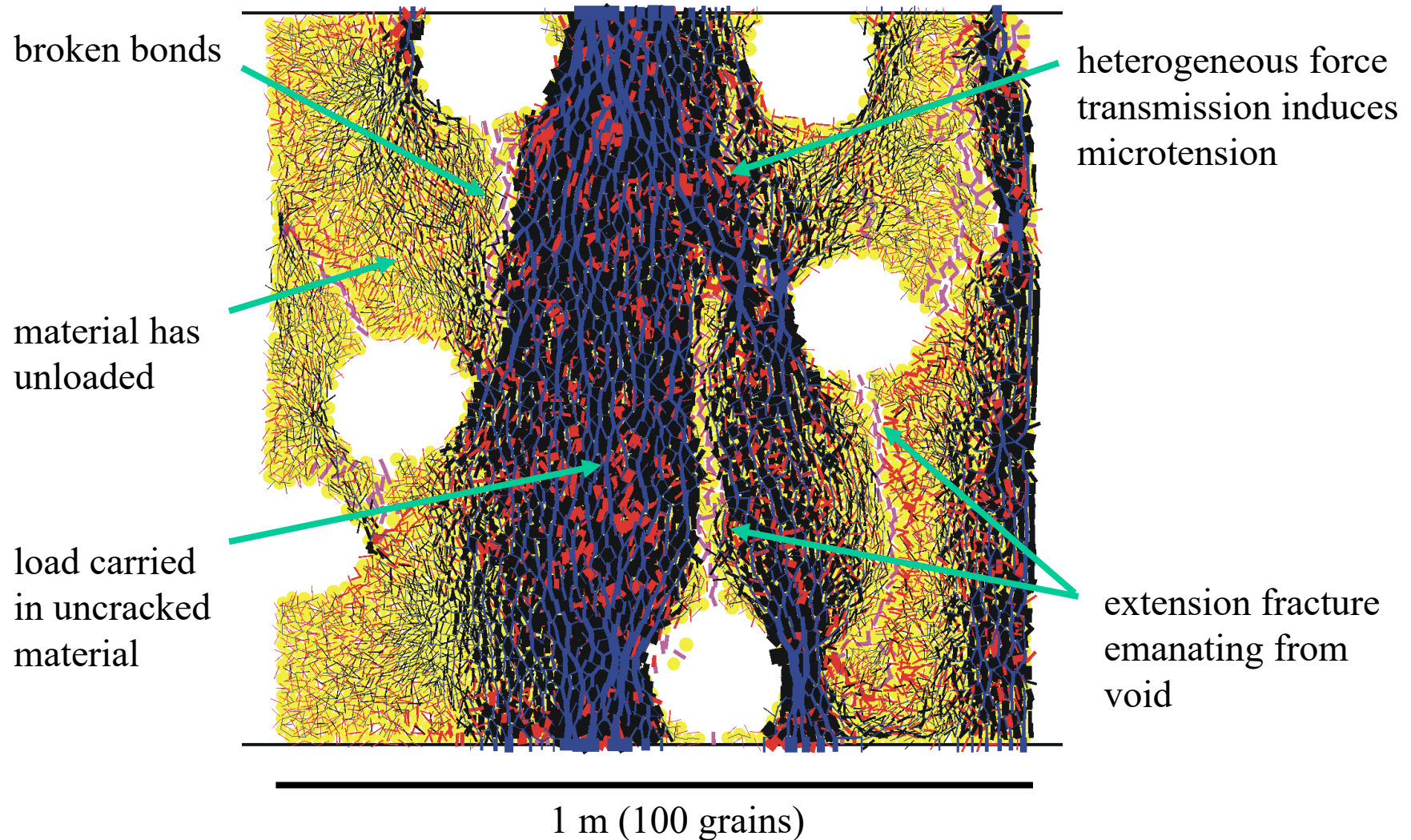
blue : compression between grains  
black/red : compression/tension in cement

# Essential Features of a BPM



Microstructural mechanisms in cemented granular material to induce **microtension** and **bond breakage**.

# Essential Features of a BPM



# Microstructural Physics of Intact Rock

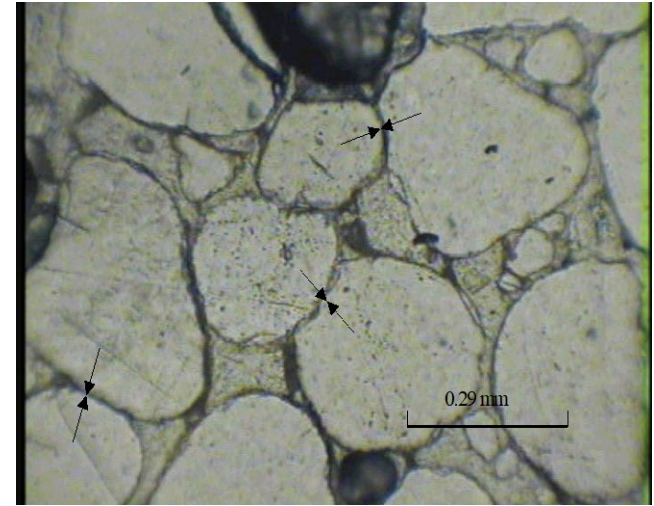
Intact rock can be viewed as an aggregate of crystals & amorphous particles joined by varying amounts of cementing materials.

Intact rock can be represented as...

Heterogeneous material comprised of cemented grains.

Much disorder in system:

- grain size, shape & packing
- grain & cement properties
- degree of cementation
- locked-in stresses



sandstone

Dittes & Labuz (2002)

Each item influences mechanical behavior, and may evolve under load application.

# Microstructural Physics of Intact Rock

Brittle mechanical properties measured:

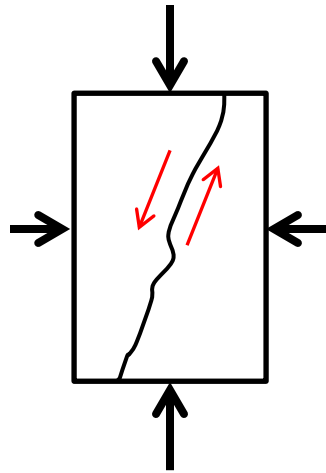
uniaxial & triaxial compression tests

tension tests

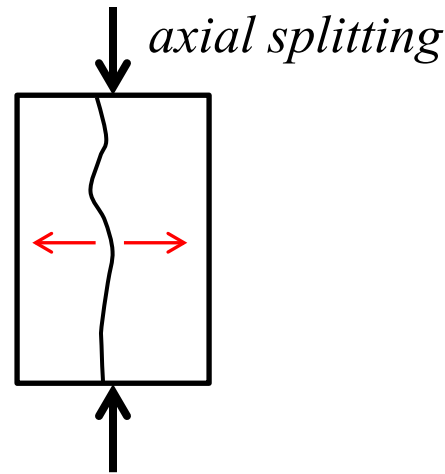
Two principal modes of brittle failure:

shear fracture

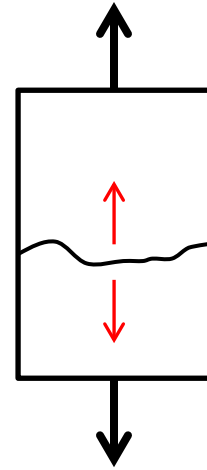
extension fracture



shear fracture

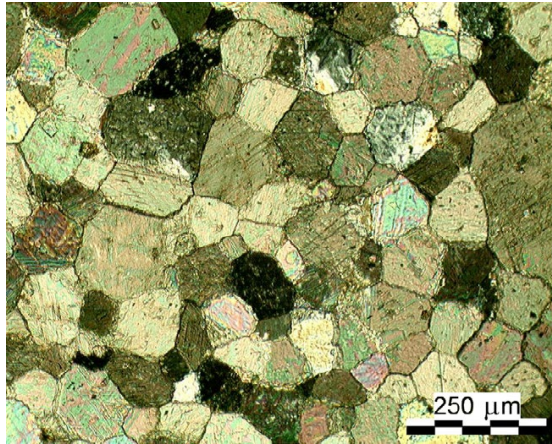


extension fracture



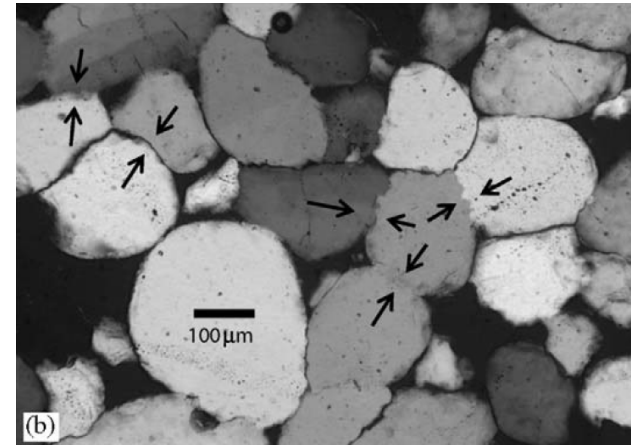
# Microstructural Physics of Intact Rock

Brittle mechanical properties are controlled by nature of pore space →  
classify intact rock as **compact** or **porous**



Bandini et al. (2012)

marble with interlocking grains



Haimson (2007)

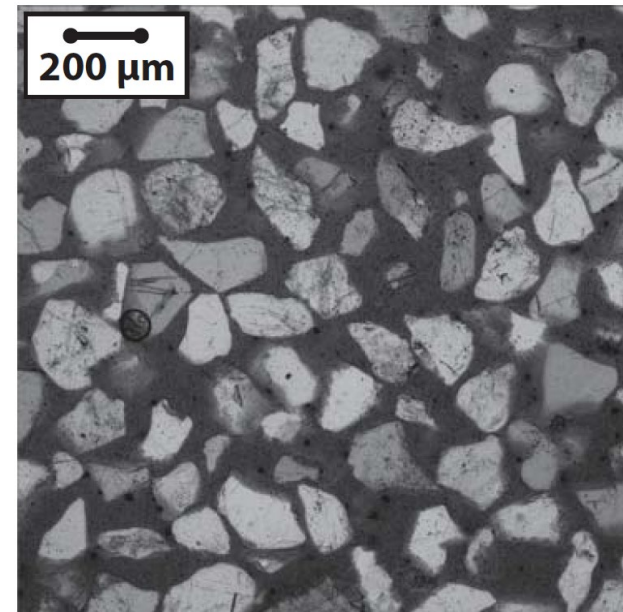
sandstone with broad grain sutures

# Microstructural Physics of Intact Rock

Compression-induced damage manifests itself as inelastic volume change (dilation or compaction) resulting from microstructural changes that are precursors to macroscopic failure.

**granular aggregate**

Deviatoric loading →  
**dilatancy**, repacking of grains



Brzesowsky et al. (2014)

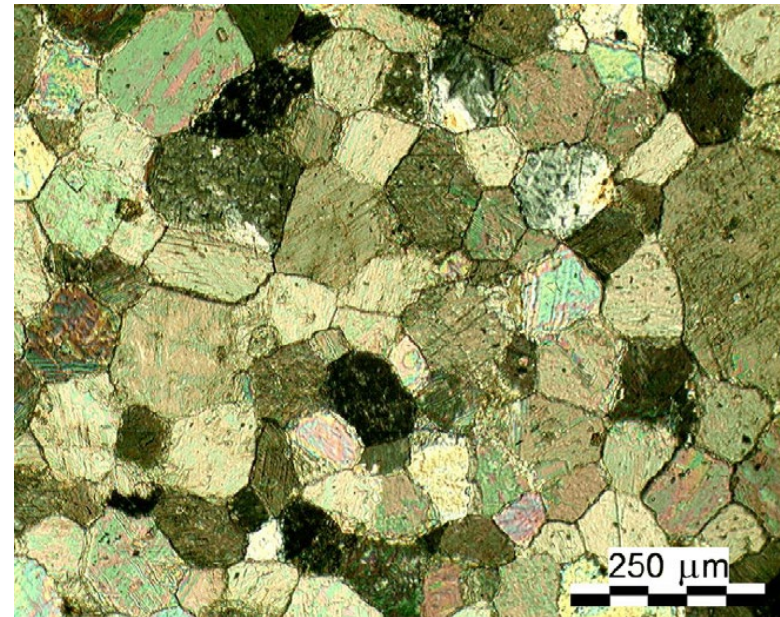
quartz sand

# Microstructural Physics of Intact Rock

Compression-induced damage manifests itself as inelastic volume change (dilation or compaction) resulting from microstructural changes that are precursors to macroscopic failure.

**compact rock**

Deviatoric loading →  
**dilatancy**, microcracking



marble

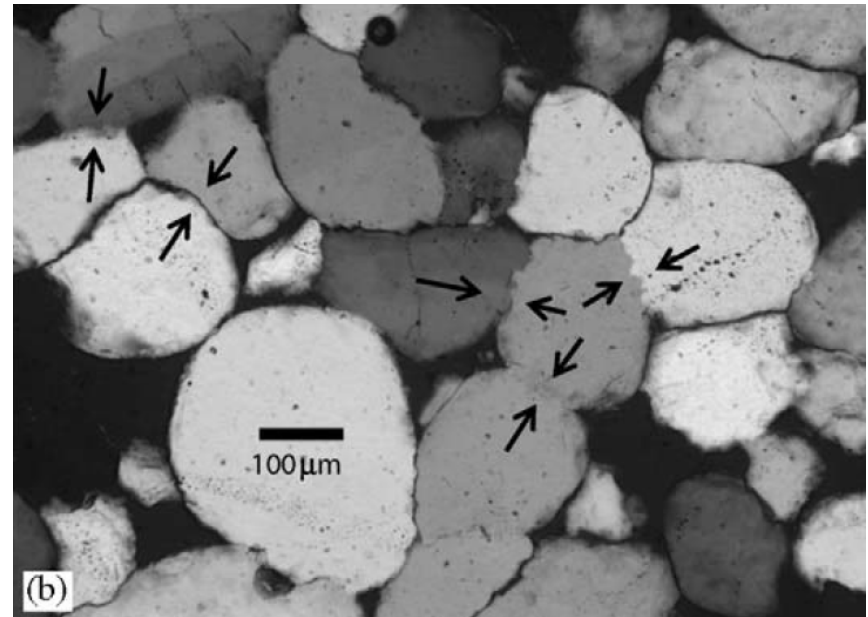
# Microstructural Physics of Intact Rock

Compression-induced damage manifests itself as inelastic volume change (dilation or compaction) resulting from microstructural changes that are precursors to macroscopic failure.

## porous rock

Hydrostatic loading →  
**compactancy**, grain crushing

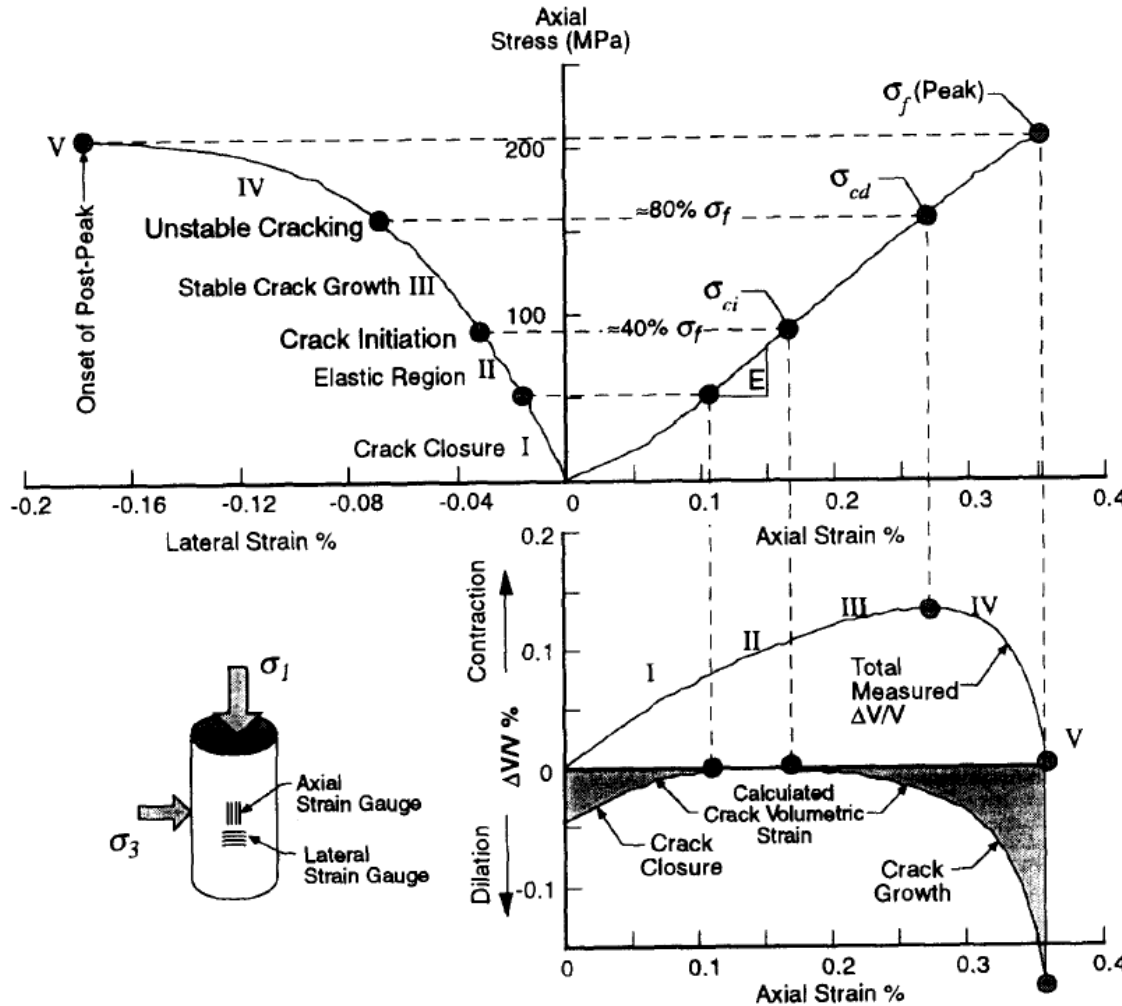
Deviatoric loading →  
**dilatancy**, microcracking  
OR  
**compactancy**, brittle grain  
crushing or plastic collapse of  
pores (shear-enhanced  
compaction)



sandstone

# Microstructural Physics of Intact Rock

Compressive behavior is described by stress-strain curves:



Four stages:

1. crack closure
2. elastic region
3. stable crack growth
4. unstable crack growth

Martin & Chandler (1994)

# Microstructural Physics of Intact Rock

Compressive behavior is **explained** in terms of flaws & heterogeneities in the rock material on the microscopic scale in which brittle fracture is viewed as a localization in the proliferation of microcracking.

It is essential to have a **realistic structural description of the rock** as a basis for...theoretical developments, and to consider the evolution of the structure during the progression of the failure.

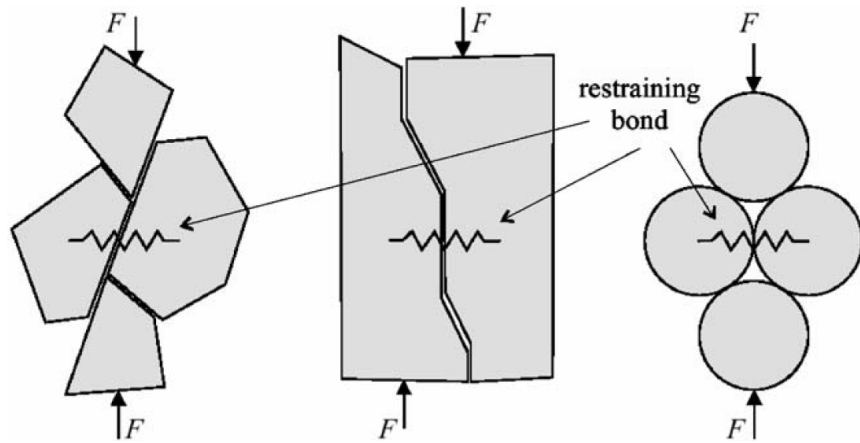
BPMs provide a **micromechanical theory of brittle failure**

- various physical models of the brittle-fracture process
- discern the effects of microstructure on macroscopic behavior

# Two Complementary Idealizations of Rock

## BPM material

(cemented granular material)

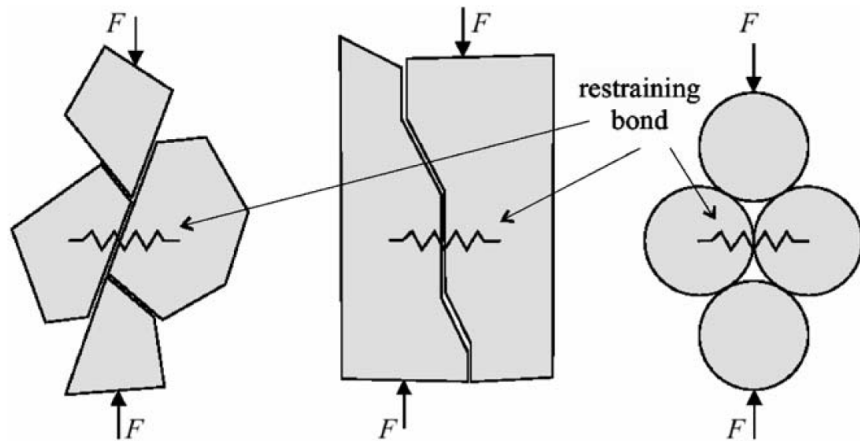


Microstructural mechanisms to induce  
microtension and bond breakage

# Two Complementary Idealizations of Rock

## BPM material

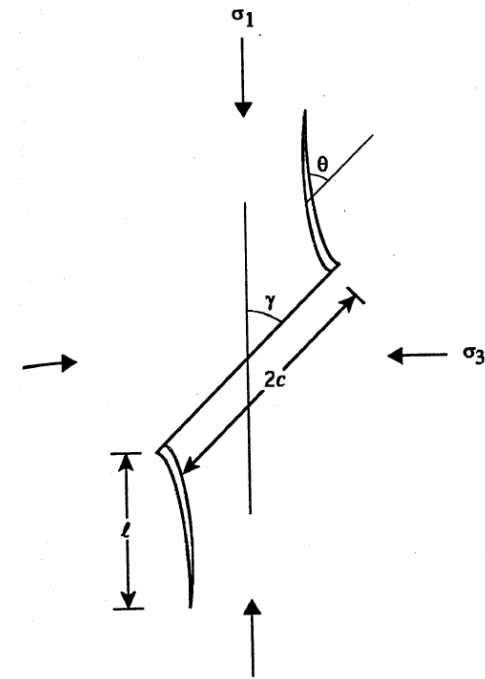
(cemented granular material)



Microstructural mechanisms to induce **microtension** and **bond breakage**

## LEFM material

(linear-elastic body with initial population of cracks)



Microstructural mechanism to induce **microtension** and **crack extension** via sliding crack & wing cracks

# Two Complementary Idealizations of Rock

Why does axial splitting occur?

It originates from local transverse tensile stresses at flaws or heterogeneities in the rock.

For both materials, the axial splits nucleate

- as wing cracks in LEFM material
- as broken bonds in BPM material

# Two Complementary Idealizations of Rock

Why does axial splitting occur?

It originates from local transverse tensile stresses at flaws or heterogeneities in the rock.

For both materials, the axial splits nucleate

- as wing cracks in LEFM material
- as broken bonds in BPM material

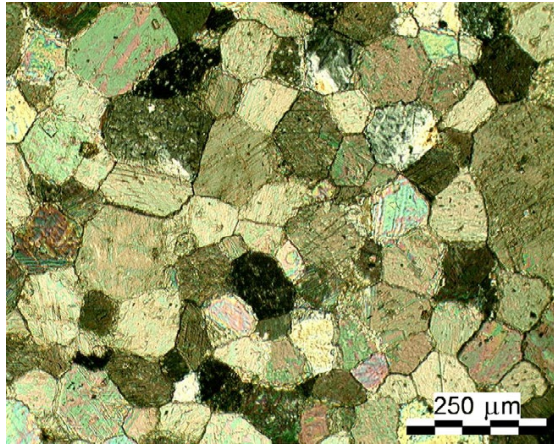
and then grow into an orientation parallel to direction of compression

- as lengthening cracks in LEFM material
- as additional broken bonds that coalesce into extension fractures in BPM material

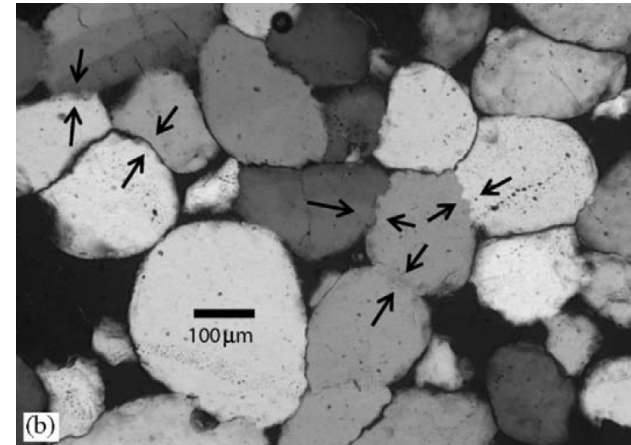
# Two Complementary Idealizations of Rock

## BPM material

- Supports microcrack nucleation as well as growth and eventual interaction
- Provides rich set of **grain-scale discontinuities** that can be related to microstructural features



marble with interlocking grains



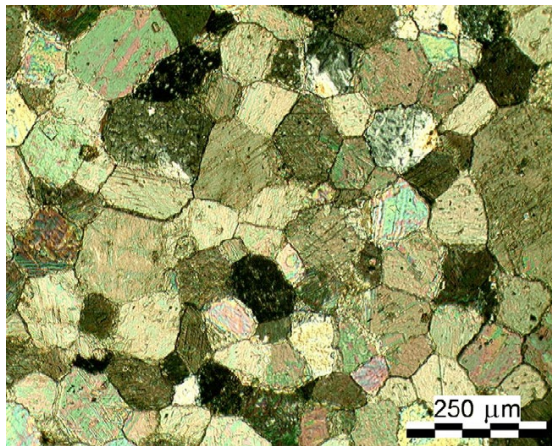
sandstone with broad grain sutures

- Grain-scale discontinuities need not be mapped into initial population of cracks

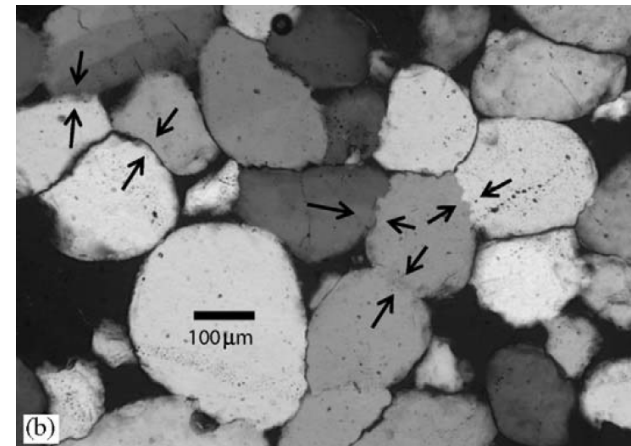
# Two Complementary Idealizations of Rock

## BPM material

- Provides rich set of **grain-scale discontinuities** that can be related to microstructural features



marble with interlocking grains



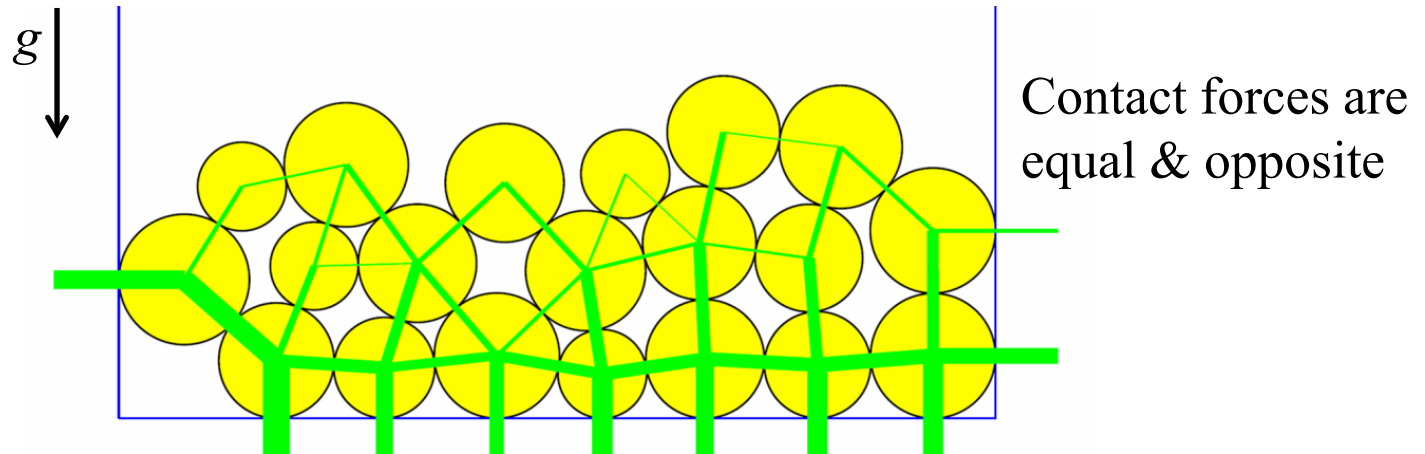
sandstone with broad grain sutures

Closer match to microstructural & structural features →  
Closer match to macroscopic behavior

# Bonded-Particle Modeling Methodology (PFC model)

PFC programs (PFC2D & PFC3D) provide a general-purpose, distinct-element modeling framework that includes a computational engine and a graphical user interface.

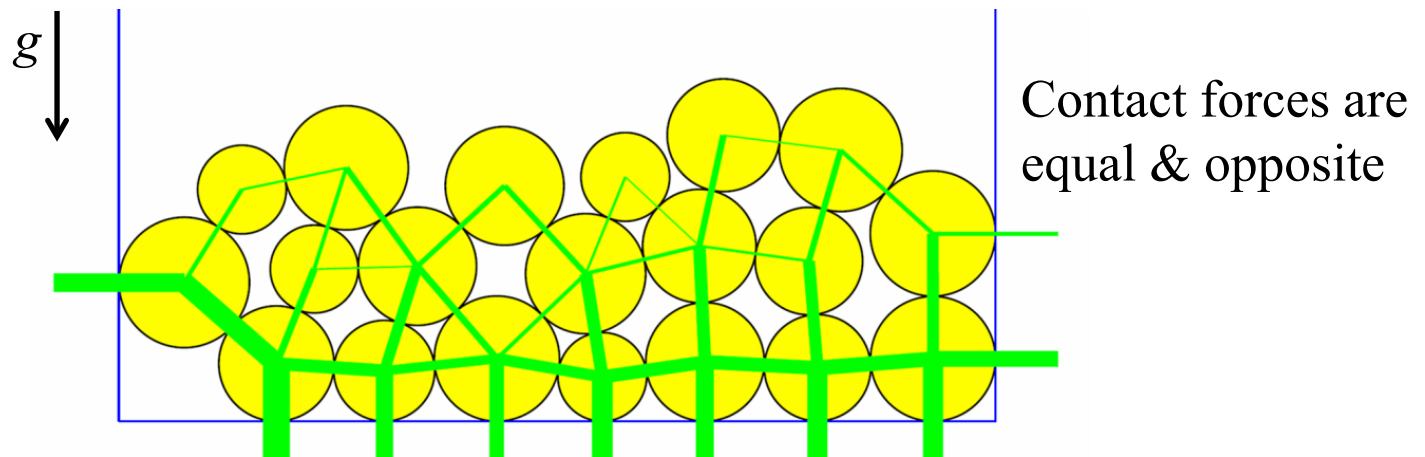
Simulate movement & interaction of many finite-sized particles via **distinct-element method**, which provides an explicit dynamic solution to Newton's laws of motion.



# Bonded-Particle Modeling Methodology (PFC model)

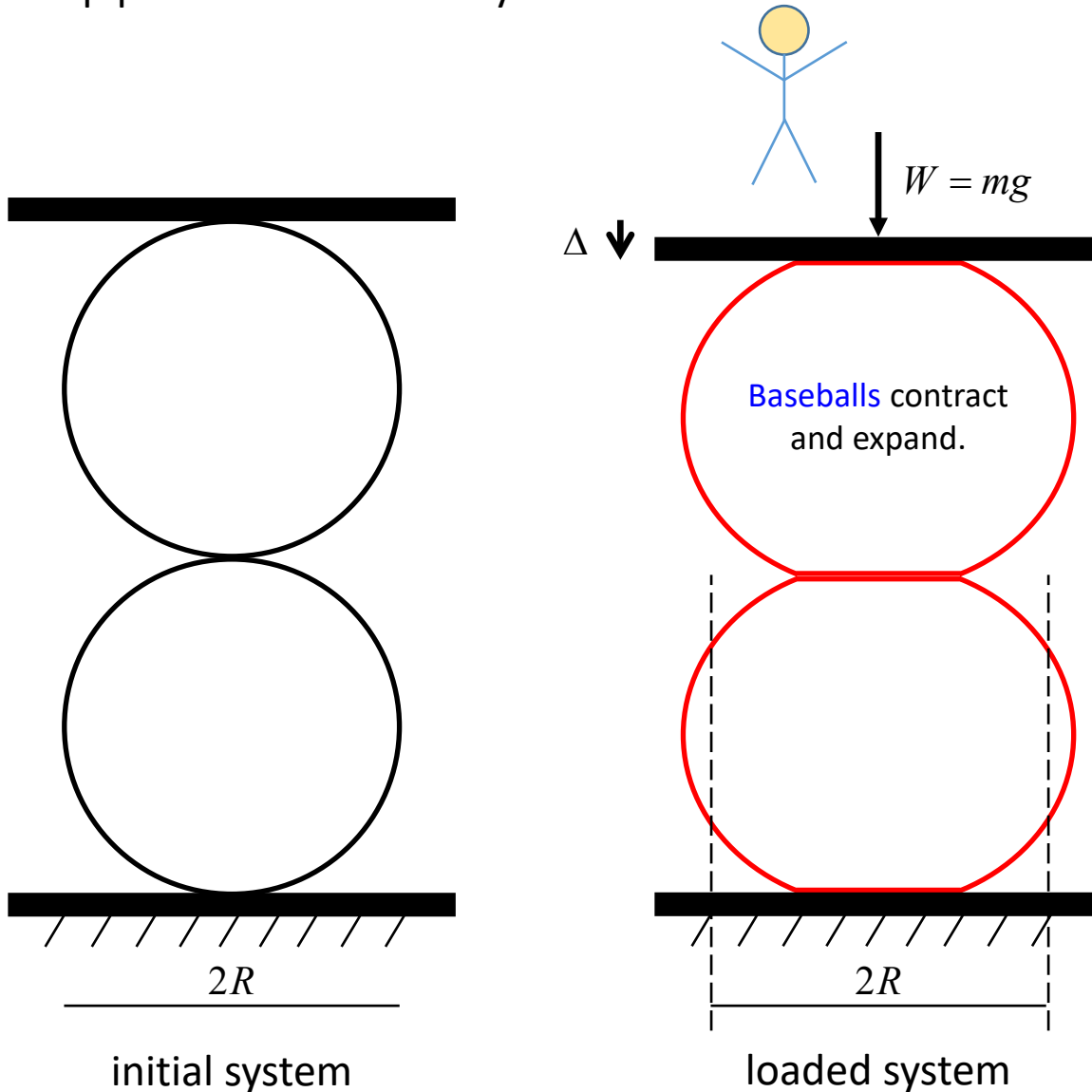
Particles are rigid bodies with finite mass that move independently of one another and can both translate and rotate. Particles interact at pair-wise contacts by means of internal force and moment.

Contact mechanics is embodied in particle-interaction laws that employ a **soft-contact approach** for which all deformation occurs at the contacts between the rigid bodies. The particle-interaction law (contact model) updates the internal force and moment.



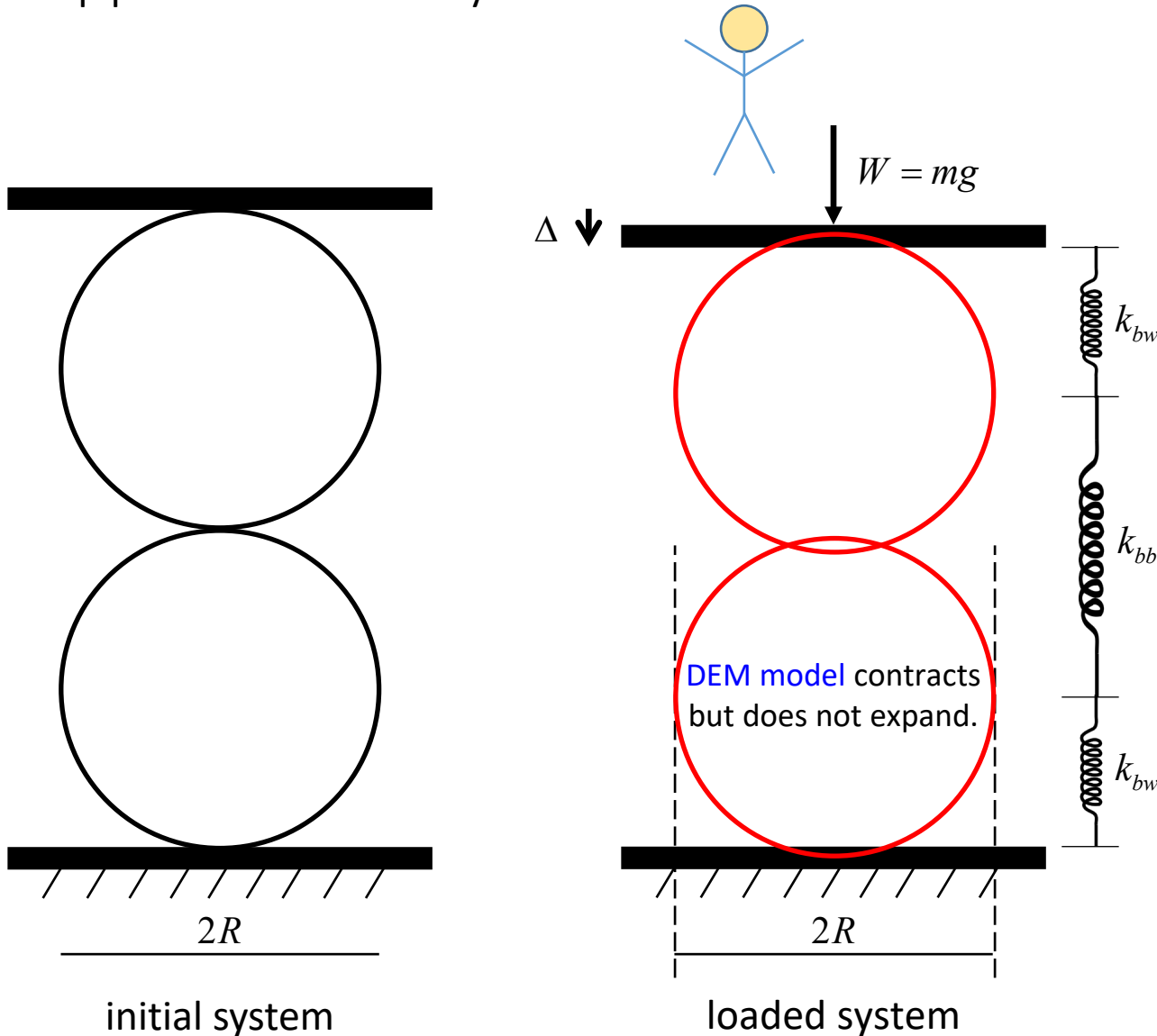
# soft-contact approach

Consider the system of me standing on two baseballs, pressed between steel plates. Top plate moves down by  $\Delta$ .



# soft-contact approach

Consider the system of me standing on two baseballs, pressed between steel plates. Top plate moves down by  $\Delta$ .



DEM model employs a “soft contact” approach:

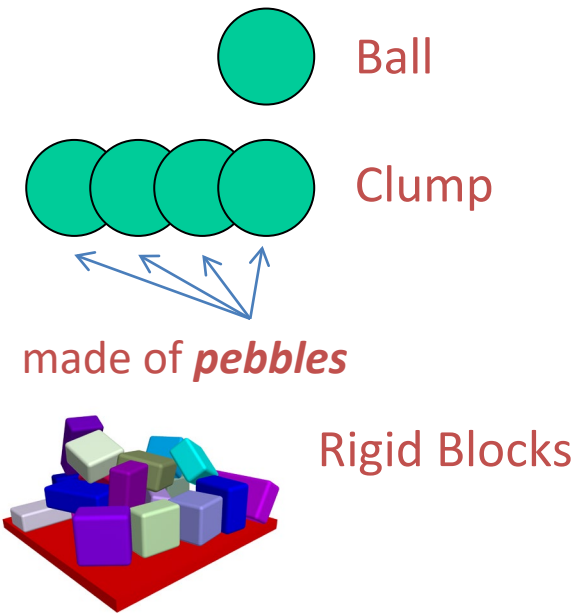
all deformation occurs at the contacts between the rigid bodies.

# Bonded-Particle Modeling (PFC model)

PFC model provides four basic entities:

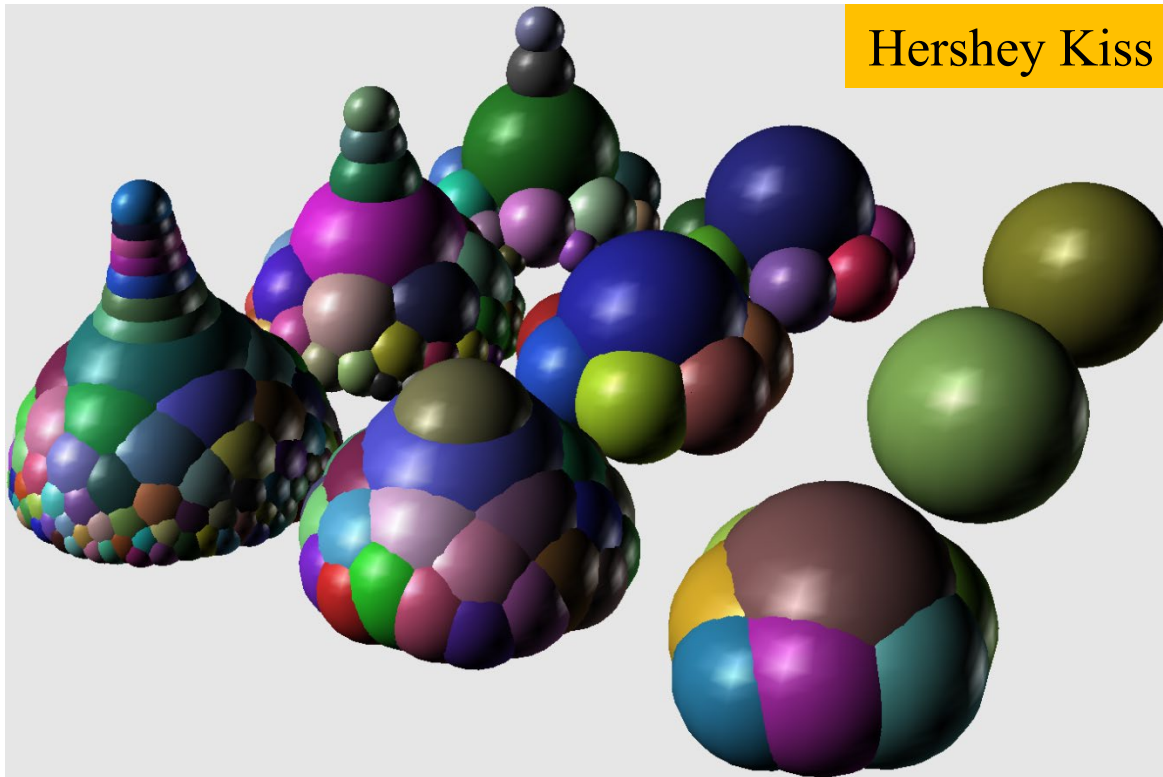
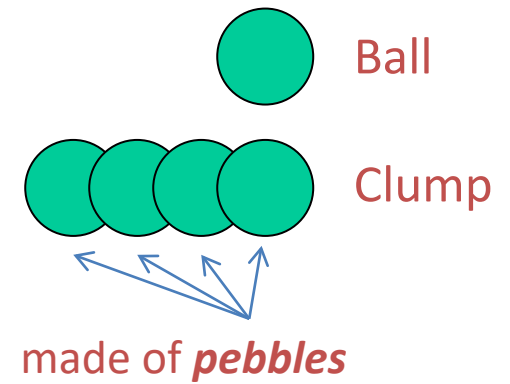
balls, clumps & rigid blocks

- obey laws of motion
- interact with one another and with walls



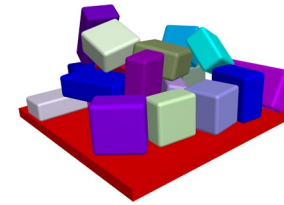
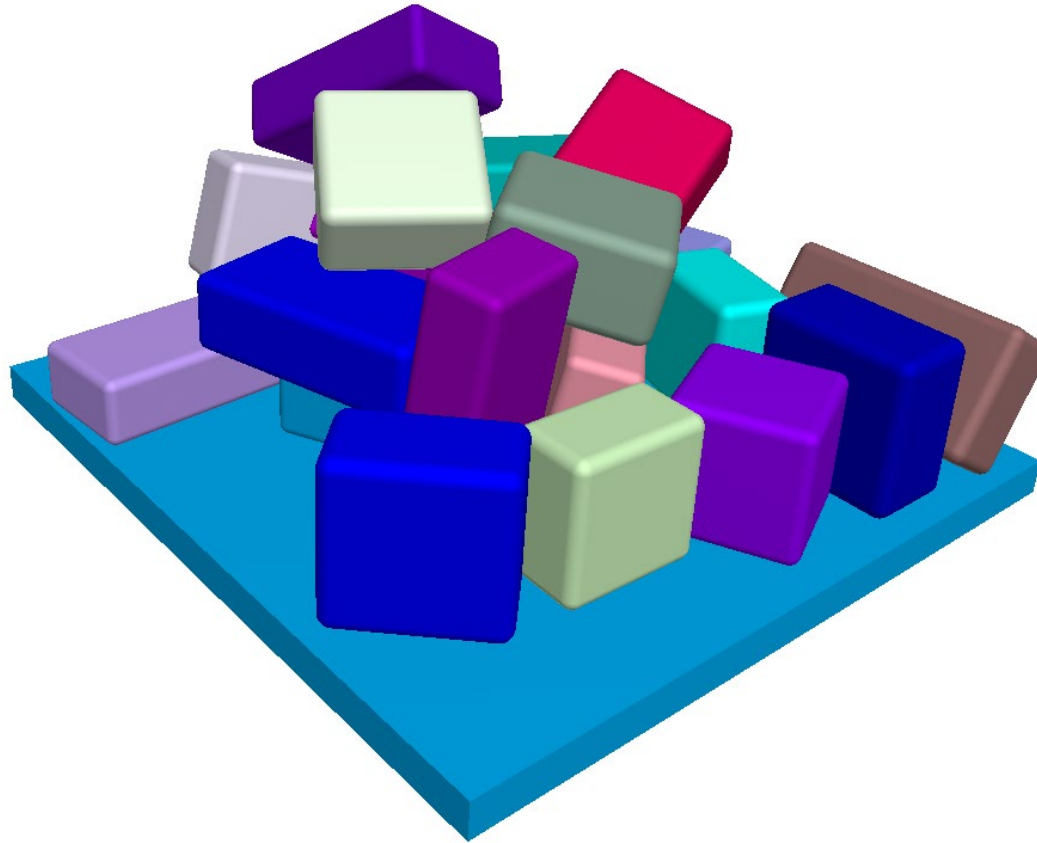
# What is a clump?

- Group of pebbles that behaves as rigid body with deformable boundary.
- Provides generalized particle shapes.



# What is a rigid block?

- Convex polyhedron with rounded edges.
- Granular: angular shapes, good interlock
- Solid: zero-porosity intact rock (BBM)



Rigid Blocks

# Bonded-Particle Modeling (PFC model)

PFC model provides four basic entities:

**balls, clumps & rigid blocks**

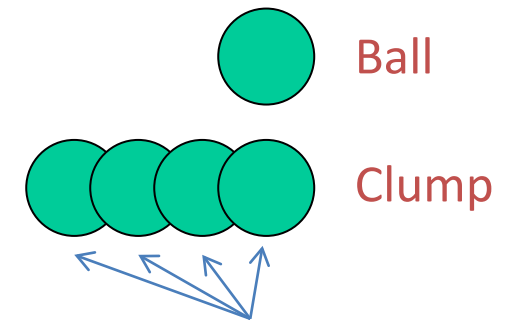
- obey laws of motion
- interact with one another and with walls

**walls**

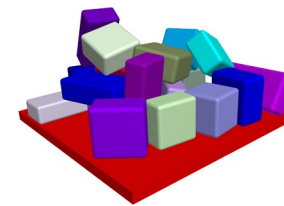
- do not obey laws of motion
- used to apply velocity boundary conditions
- interact *only* with balls, clumps & rigid blocks
- made of facets

These entities interact at **contacts**.

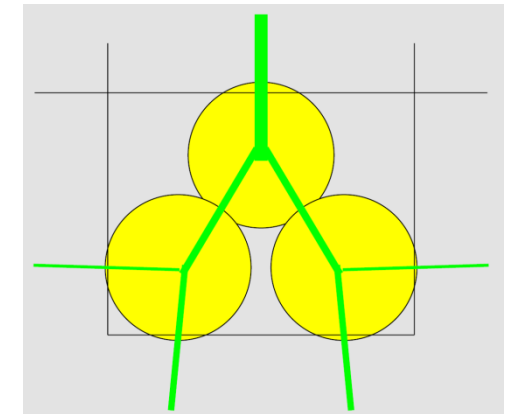
Each contact stores force & moment that act on the two contacting entities.



made of *pebbles*



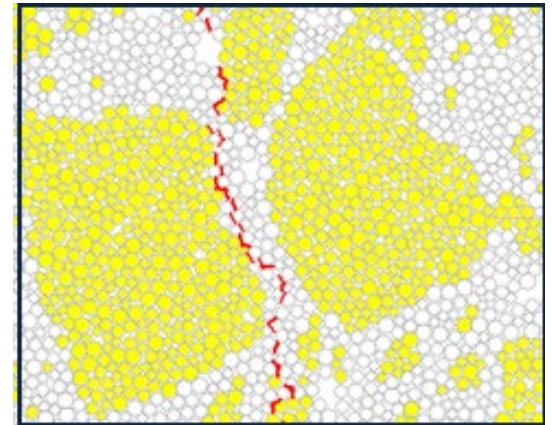
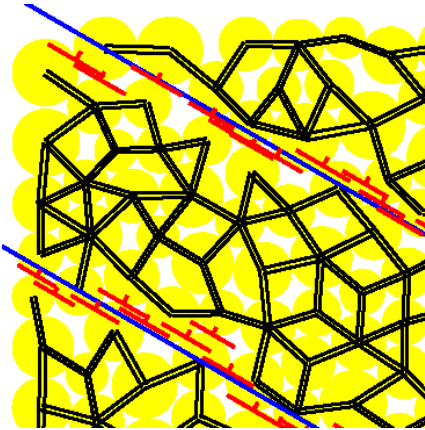
Rigid Blocks



# Microstructural Models Provided by BPM

Rich variety of models, described and classified

- base material itself (intact rock)
- overlay joints, voids & material regions



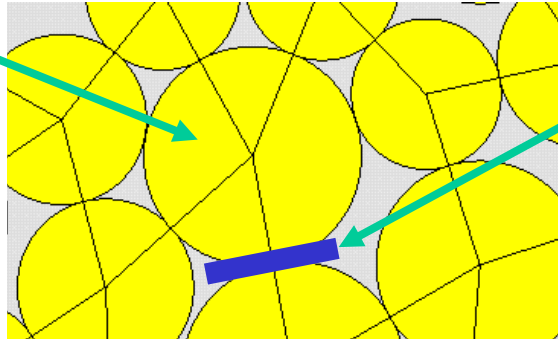
Provide wide range of rock behaviors that encompass

- compact & porous rock at both an intact and rock-mass scale

# Microstructural Models Provided by BPM

Base material itself can serve as model of intact rock

- rigid **grains** joined by deformable & breakable **cement**



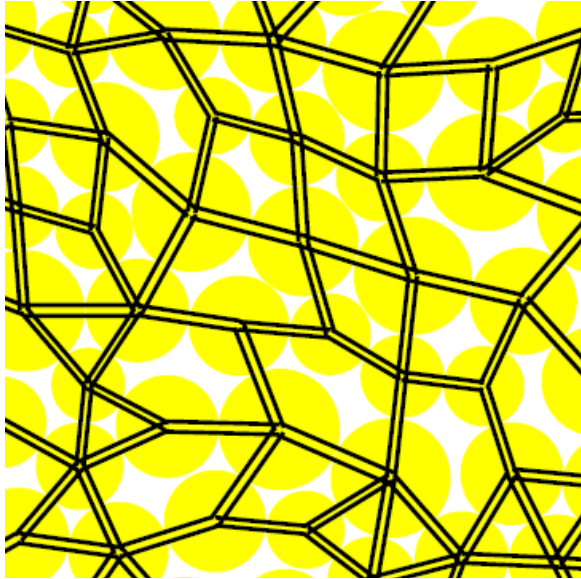
**grains** can be balls, clumps or rigid blocks

**cement** can be

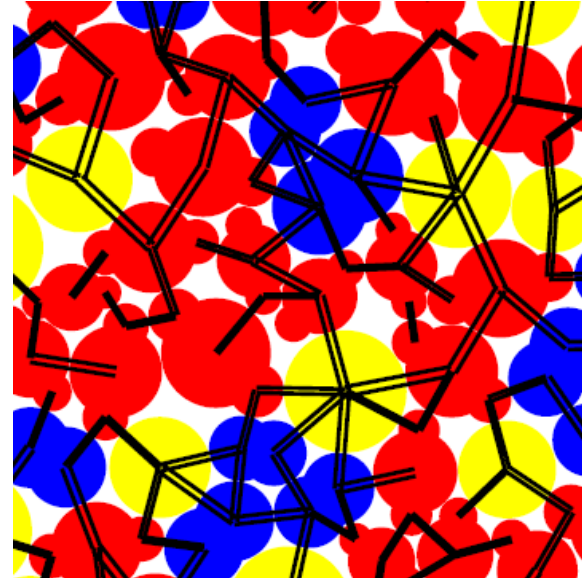
- **contact-bonded** contact
- **parallel-bonded** contact      Also **soft-bonded** contact
- **flat-joint** contact

When bond breaks, behaves as **linear** contact.

grains can be balls, clumps. . .



circular grains  
(balls)

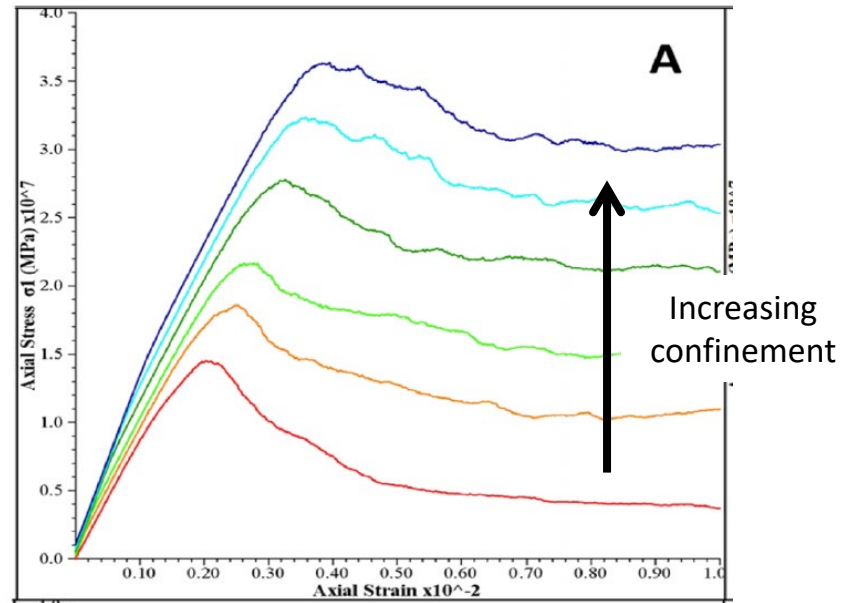


mixed-shape grains  
(balls & clumps)

Bonded material consisting of grains (with balls in yellow and clumps in blue and red) and cement (drawn as pairs of black lines).

**grains** can be balls, clumps or **rigid blocks**

## Bonded Tetrahedral Grains



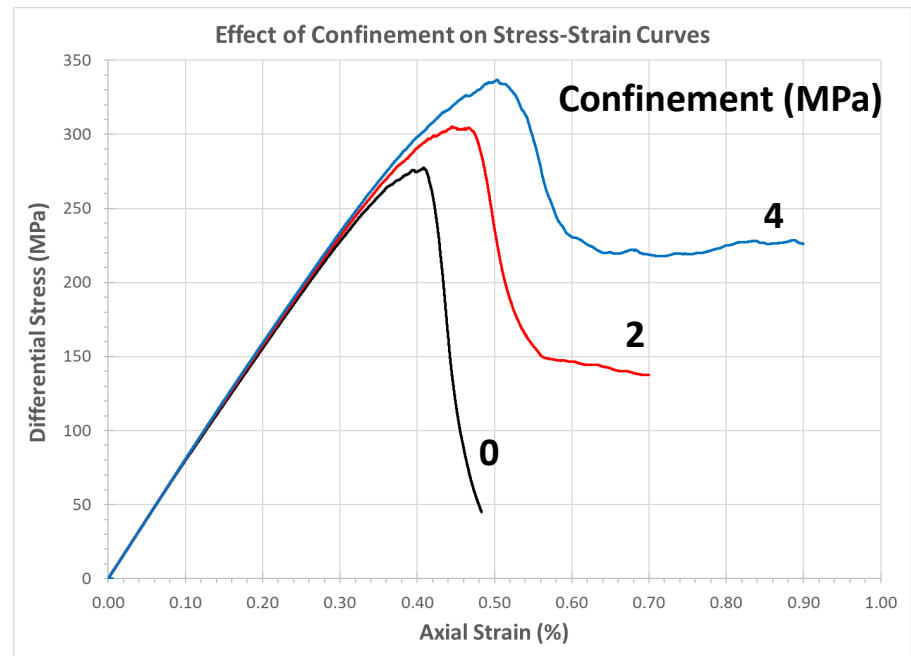
Bonded-block model consisting of grains (tetrahedrons) and cement between grain faces subjected to unconfined-compression test.

**grains** can be balls, clumps or **rigid blocks**

## Bonded Voronoi Grains



### Triaxial Tests



Bonded-block model consisting of grains (Voronoi cells) and cement between grain faces subjected to unconfined-compression test.

**cement** can be

- **contact-bonded** contact
- **parallel-bonded** contact      Also **soft-bonded** contact
- **flat-joint** contact

When bond breaks, behaves as **linear** contact.

---

It is the type of contact model at the grain-grain contacts that defines the PFC material as being linear, contact-bonded, parallel-bonded, soft-bonded or flat-jointed.

Let's examine each contact model:

Linear Model

Linear Contact Bond Model

Linear Parallel Bond Model

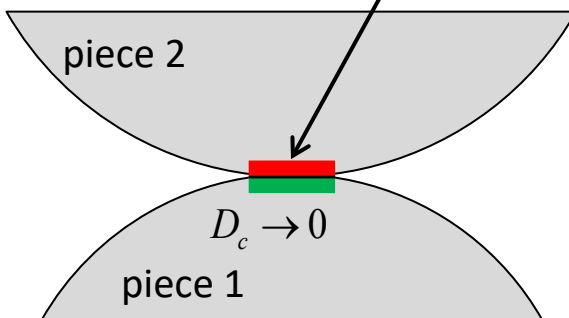
Soft-Bond Model

Flat-Joint Model

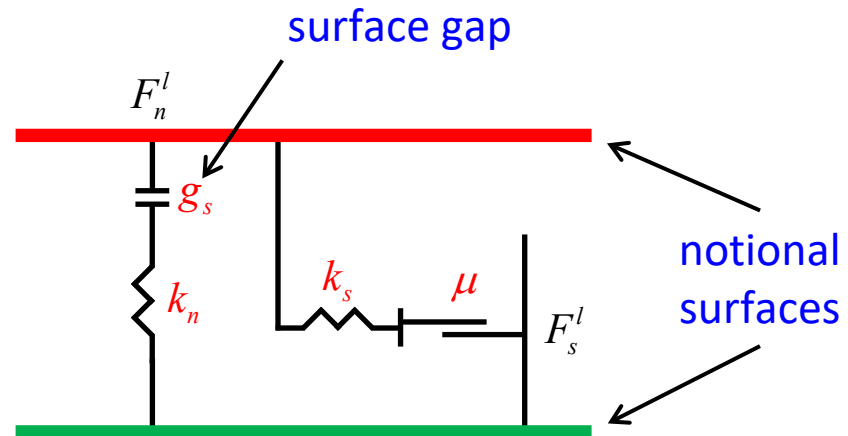
# linear contact (behavior summary)

The linear model with a reference gap of zero corresponds with the model of Cundall & Strack (1979).

Linear force ( $\mathbf{F}^l$ ), linear elastic  
(no tension) and frictional.

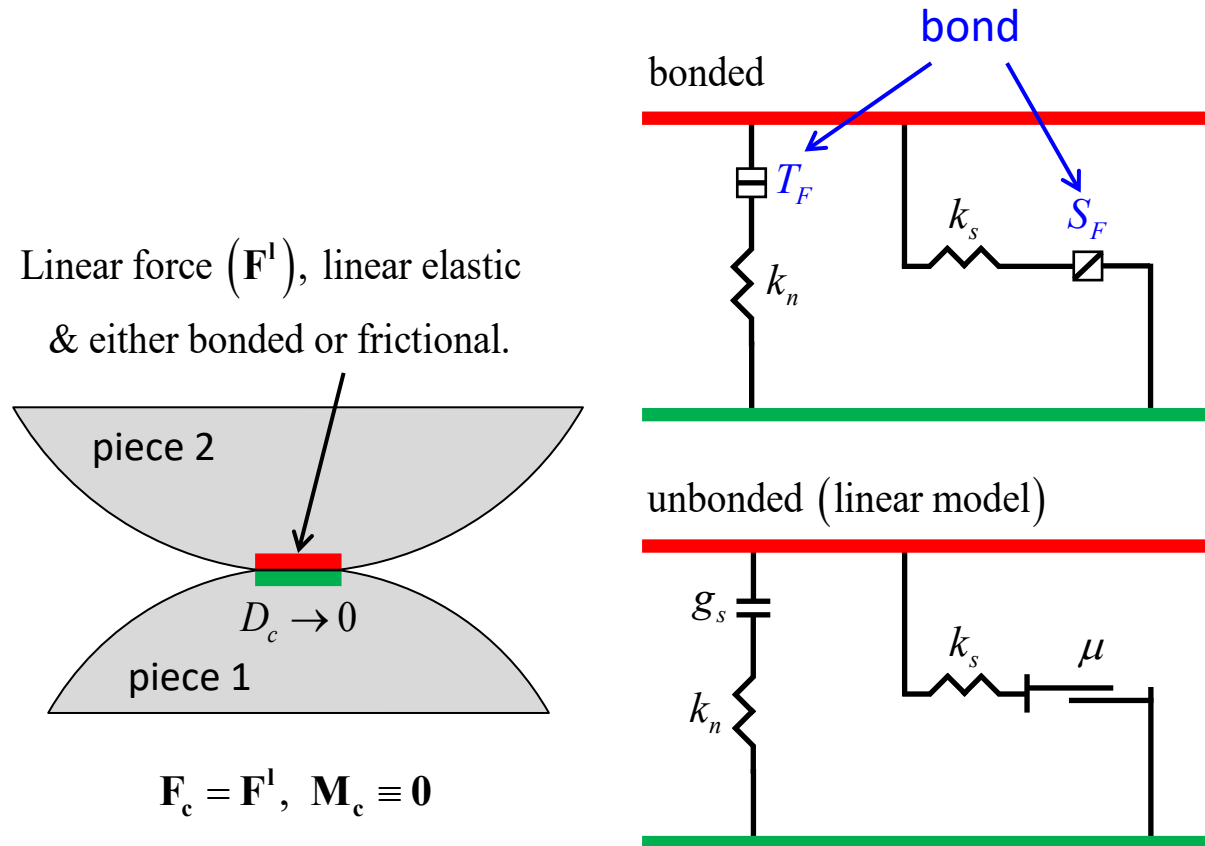


$$\mathbf{F}_c = \mathbf{F}^l, \mathbf{M}_c \equiv \mathbf{0}$$



# contact-bonded contact (behavior summary)

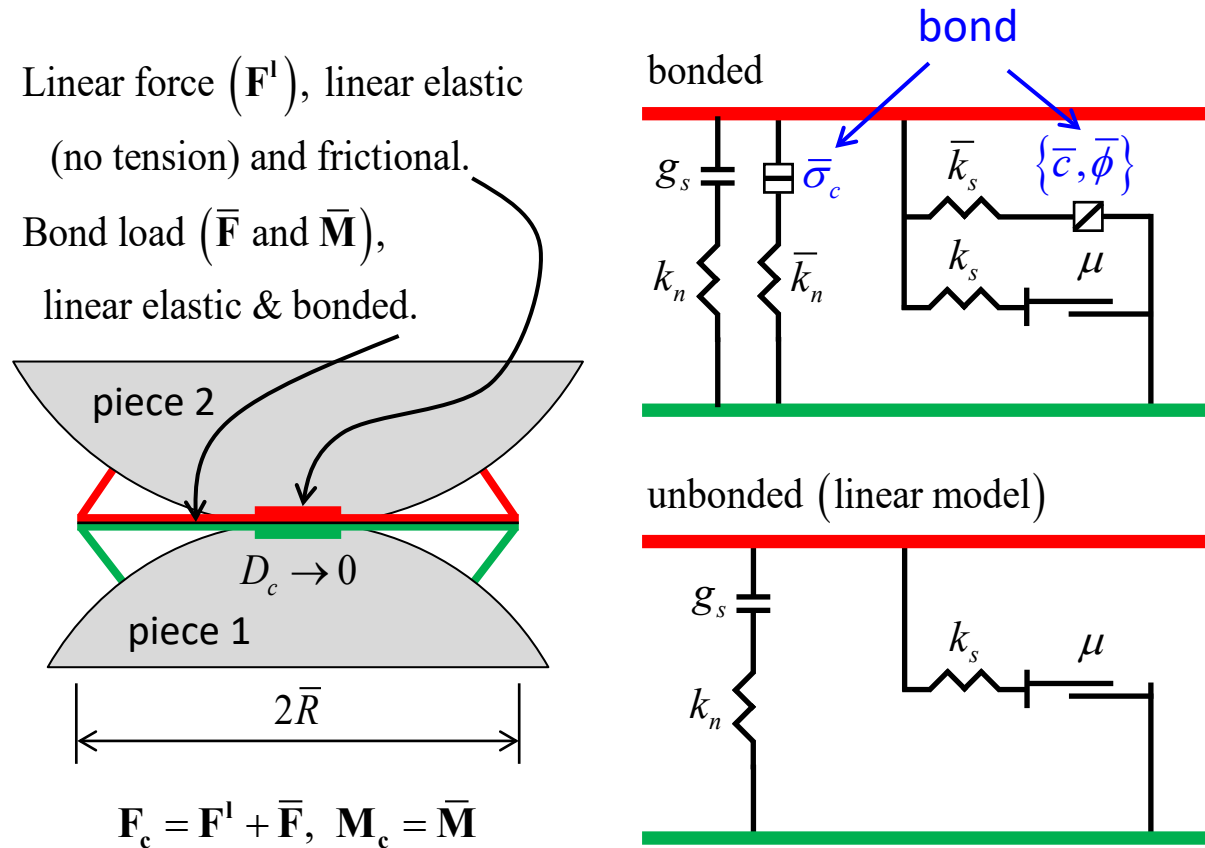
Add a spot of glue to the linear contact model, no slip while bond is intact.



# parallel-bonded contact (behavior summary)

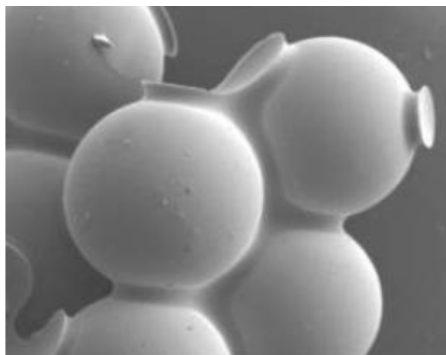
Two interfaces.

First interface is same as linear model. Second interface is finite-sized.

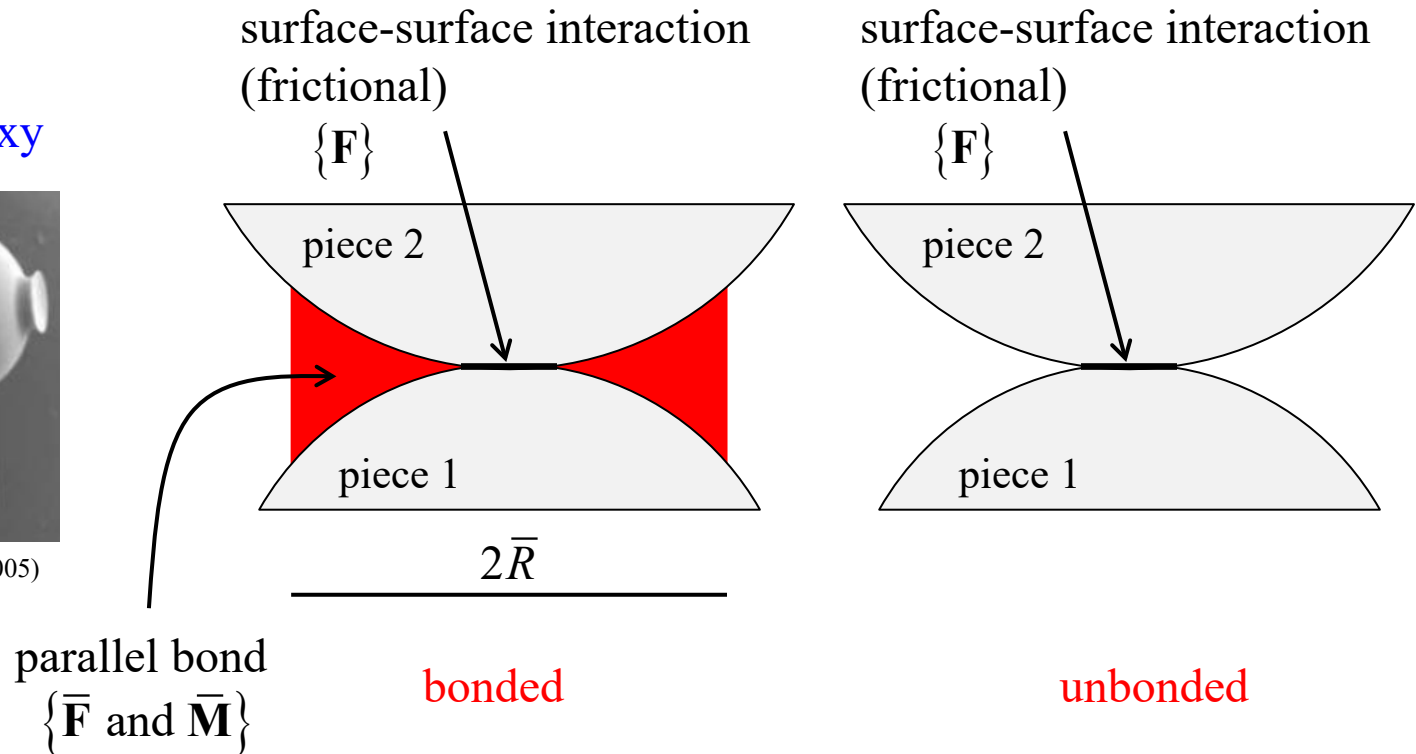


# parallel-bonded contact (behavior summary 2)

Glass beads  
cemented with epoxy

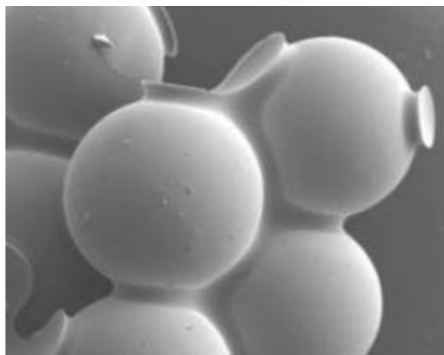


Holt et al. (2005)

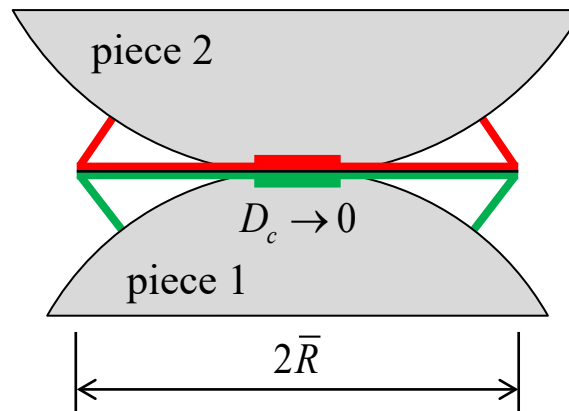


# parallel-bonded contact (behavior summary 3)

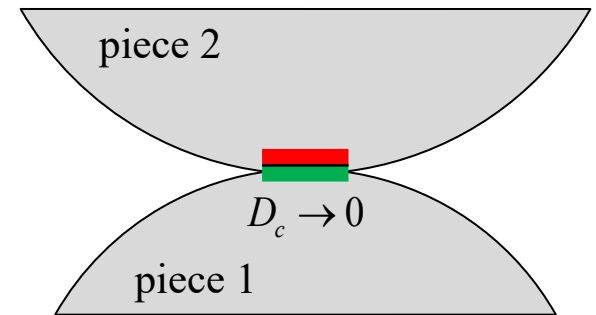
Glass beads  
cemented with epoxy



Holt et al. (2005)



bonded



unbonded

Bond breaks → it is removed, no longer resists relative rotation.

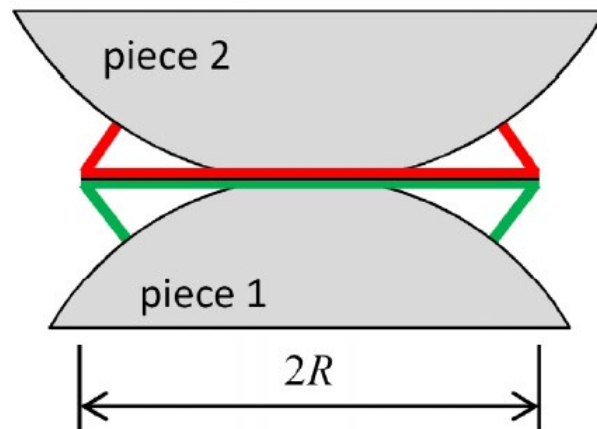
# soft-bonded contact (behavior summary)

Like parallel bond with tensile softening.  
When unbonded, has rolling resistance.

Dashpot force ( $\mathbf{F}^d$ ), not shown.

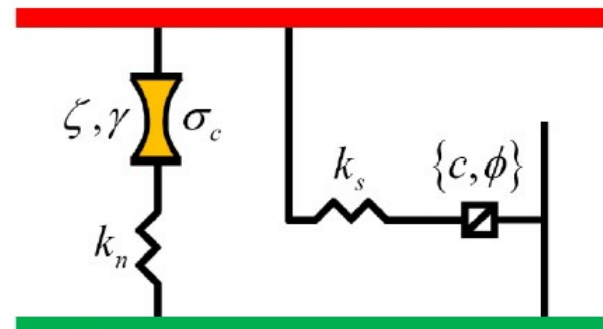
Unbonded: elastic (no tension),  
frictional with rolling resistance.

Bonded: elastic with  
tensile softening

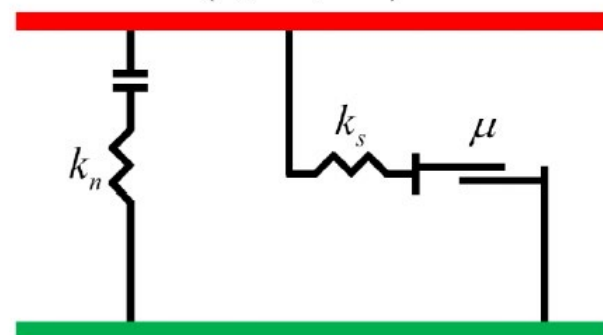


$$\mathbf{F}_c = \mathbf{F}^d + \mathbf{F}, \quad \mathbf{M}_c = \mathbf{M}$$

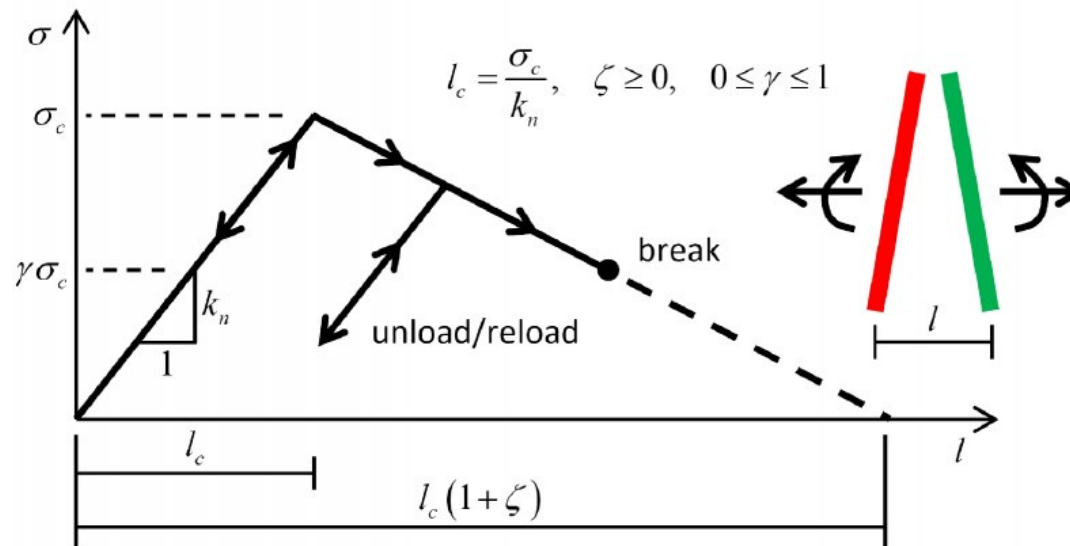
bonded



unbonded ( $\lambda_b = \lambda_t = 0$ ) rolling resistance  
is off



# soft-bonded contact (behavior summary 2)



$\sigma$  : maximum normal stress at bond periphery

$l$  : elongation at bond periphery ( $l \geq 0$ )

$l_c$  : critical bond elongation at peak strength

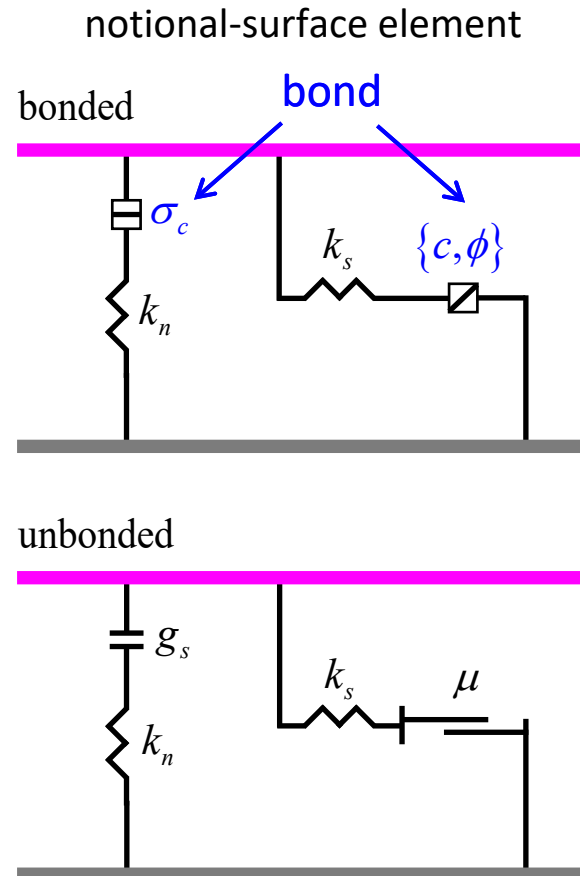
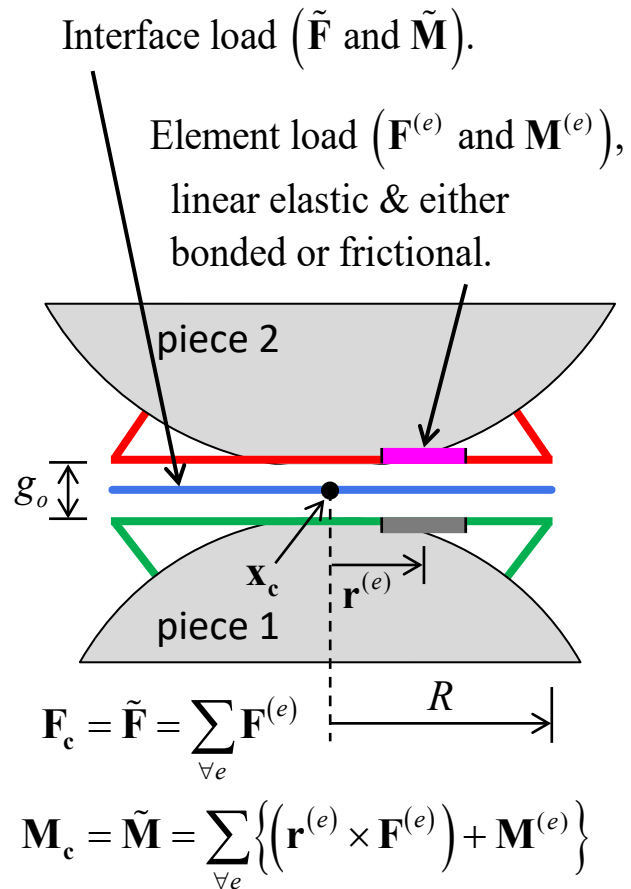
$\sigma_c$  : tensile strength [stress]

$k_n$  : normal stiffness [stress/displacement]

$\zeta$  : softening factor ( $\zeta \geq 0$ ,  $\zeta = 0$  is no softening)

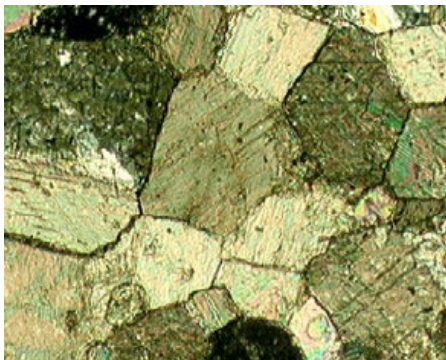
$\gamma$  : strength-reduction factor  $\begin{cases} 0 \leq \gamma \leq 1 \\ \gamma = 0 \text{ is full softening} \\ \gamma = 1 \text{ is no softening} \end{cases}$

# flat-joint contact (behavior summary)

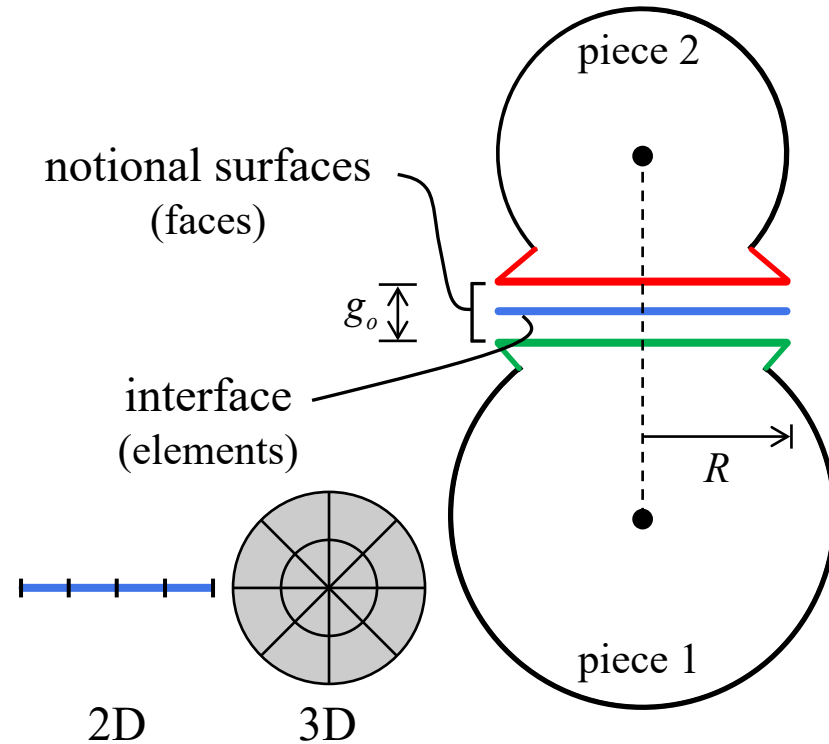


# flat-joint contact (behavior summary 2)

Marble with angular,  
interlocked grains

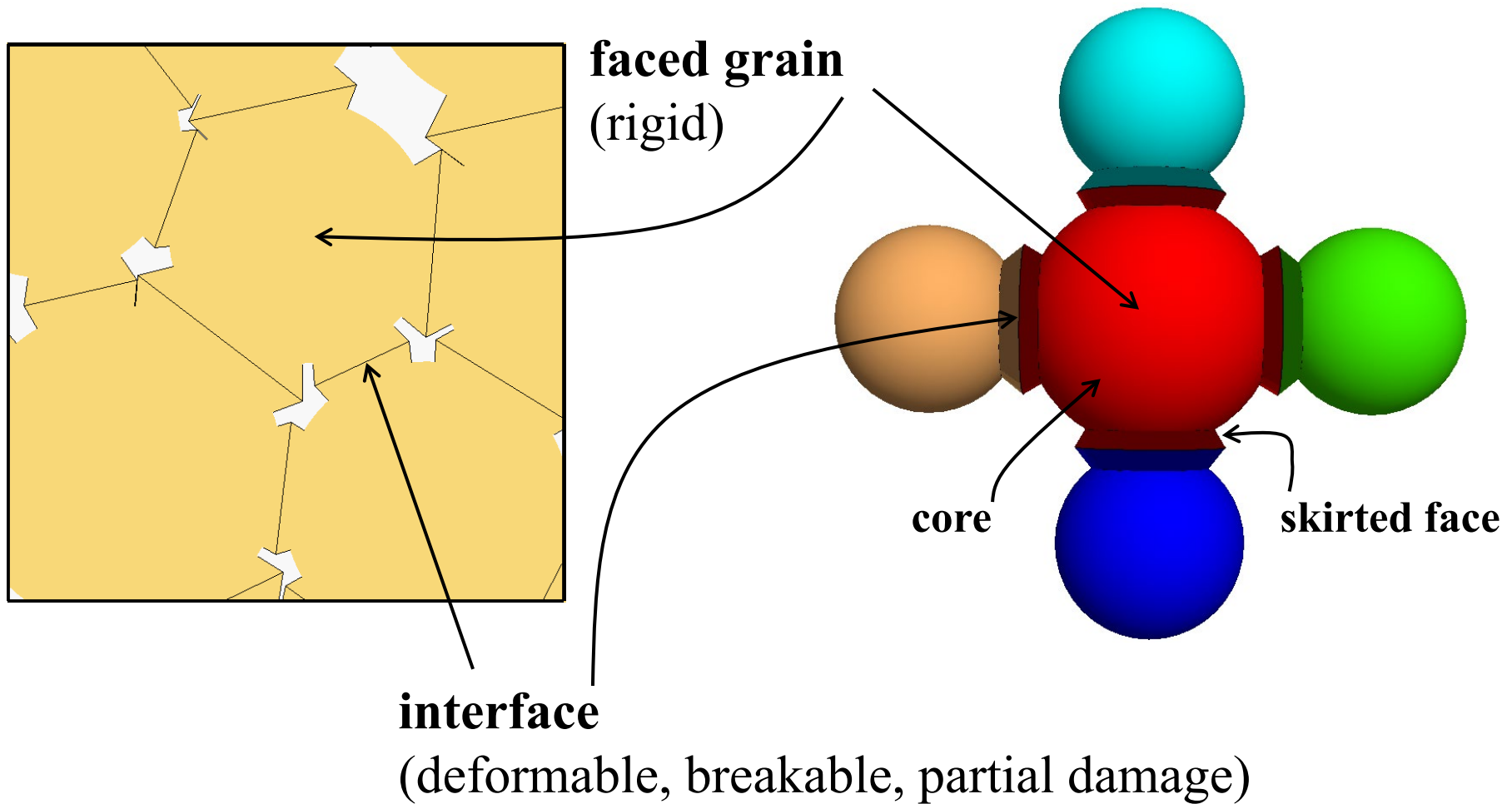


Bandini et al. (2012)



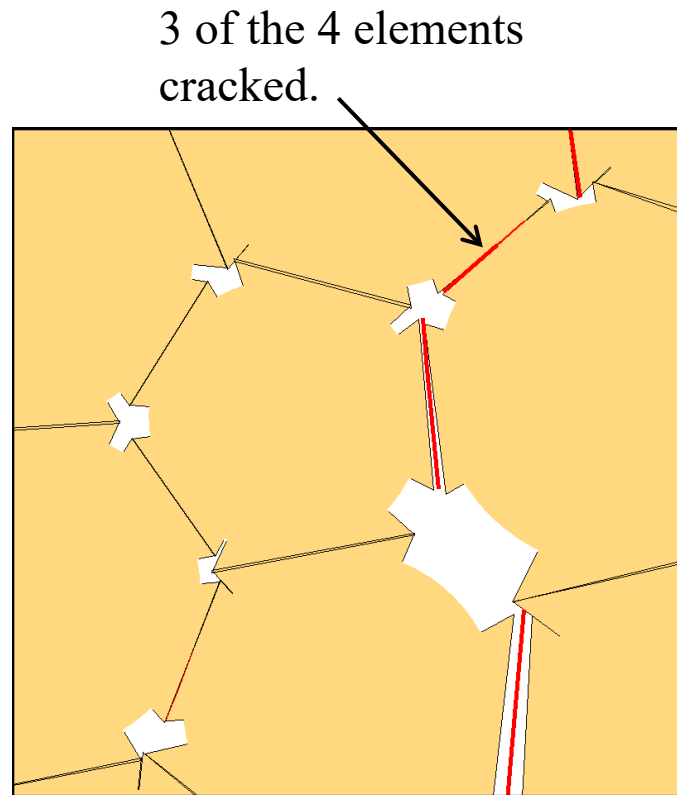
Each interface is discretized into elements that may be initially bonded, after breakage they are frictional.

# flat-joint contact (behavior summary 3)

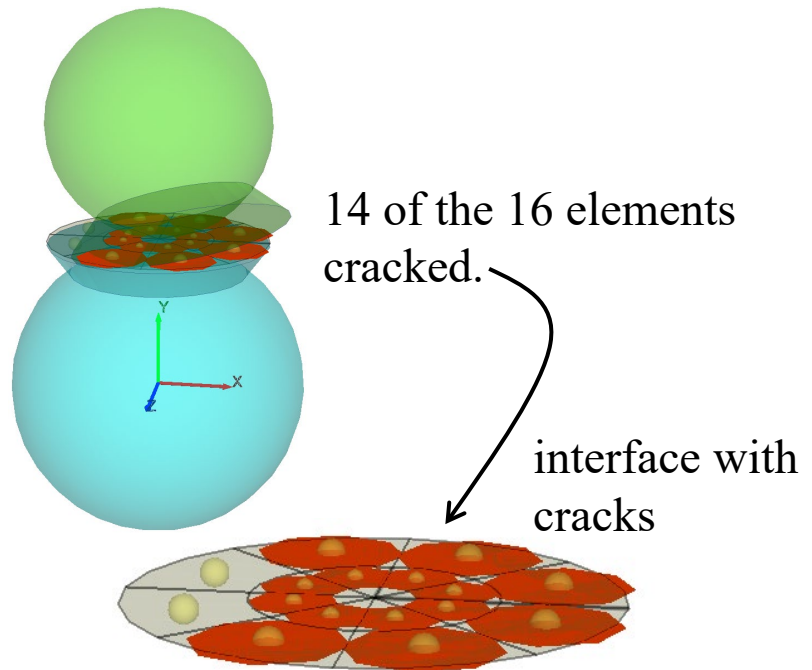


# flat-joint contact (behavior summary 4)

Bending failure with. . .

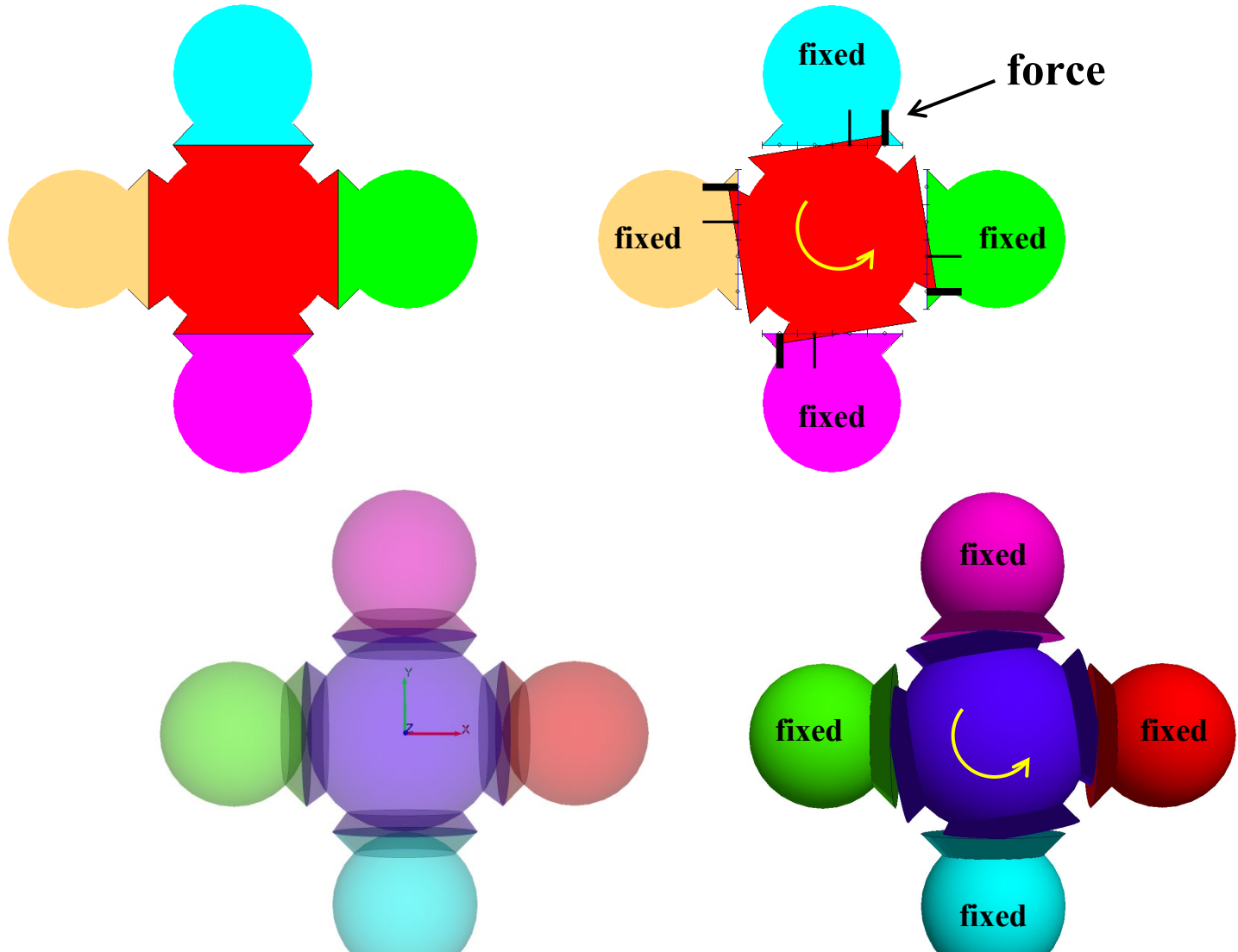


Crack thickness is proportional to gap.



The interface can sustain partial damage.

# flat-joint contact (behavior summary 5)



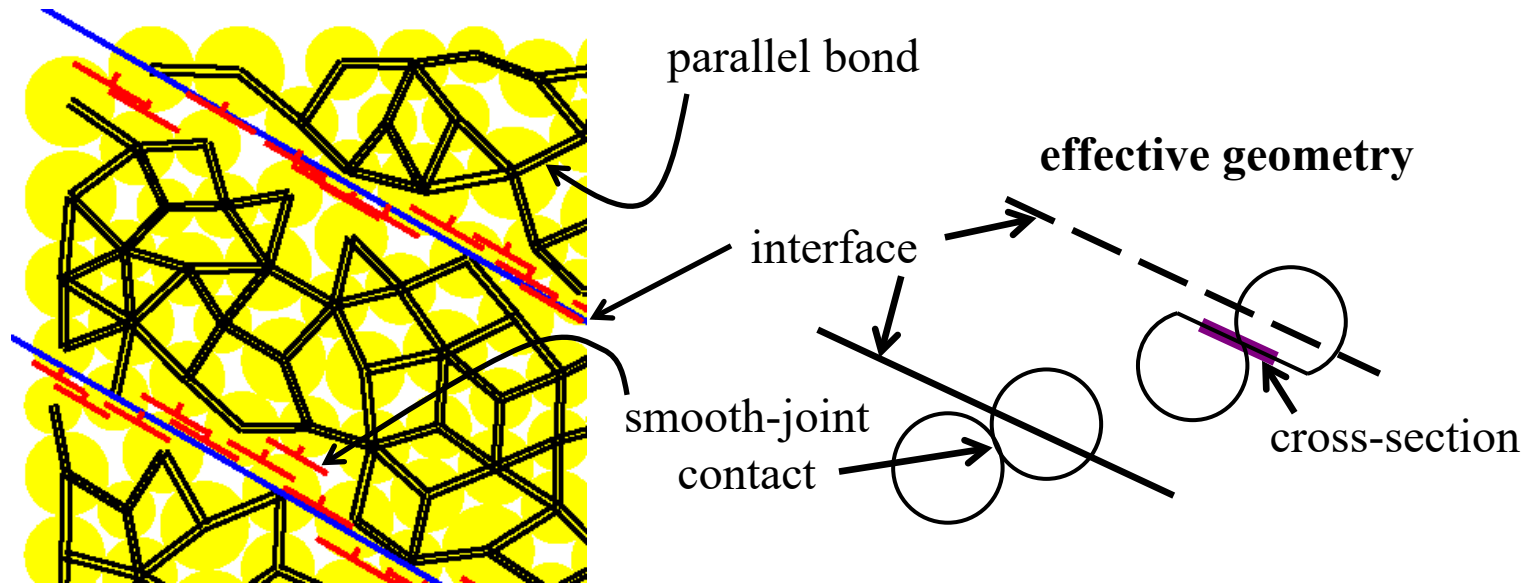
Even a fully broken interface continues to resist relative rotation.

# Microstructural Models Provided by BPM

Joints can be overlaid on base material

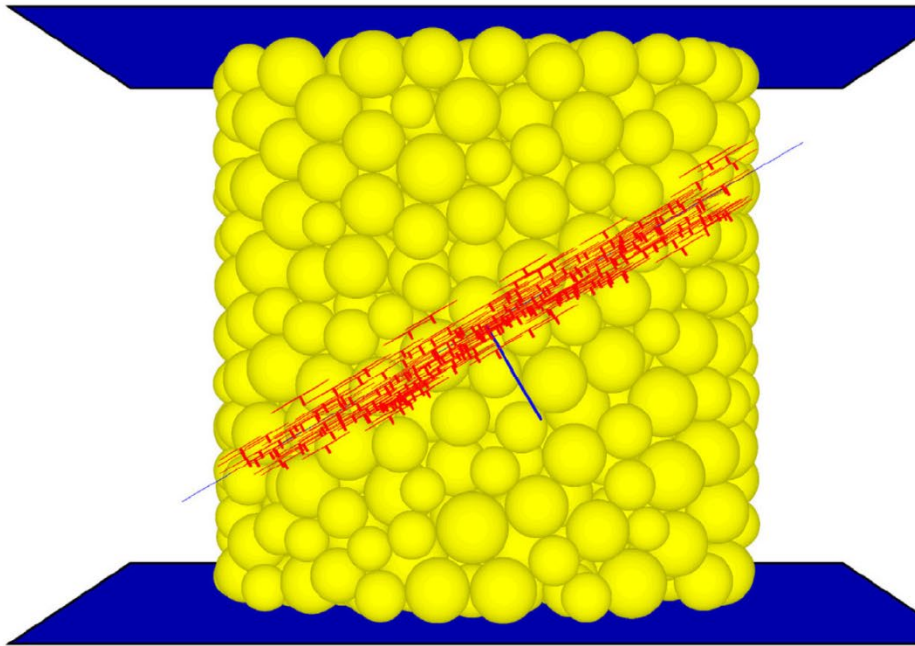
- joint behaves as **interface**

**interface** is collection of **smooth-joint** contacts

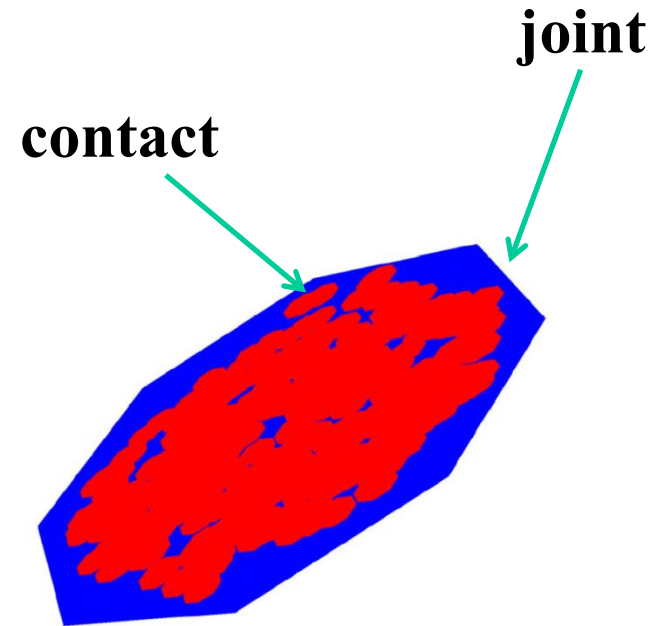


Smooth-joint contacts may be initially bonded. When bond breaks, they behave as linear contact.

# smooth-joint contact (behavior summary)



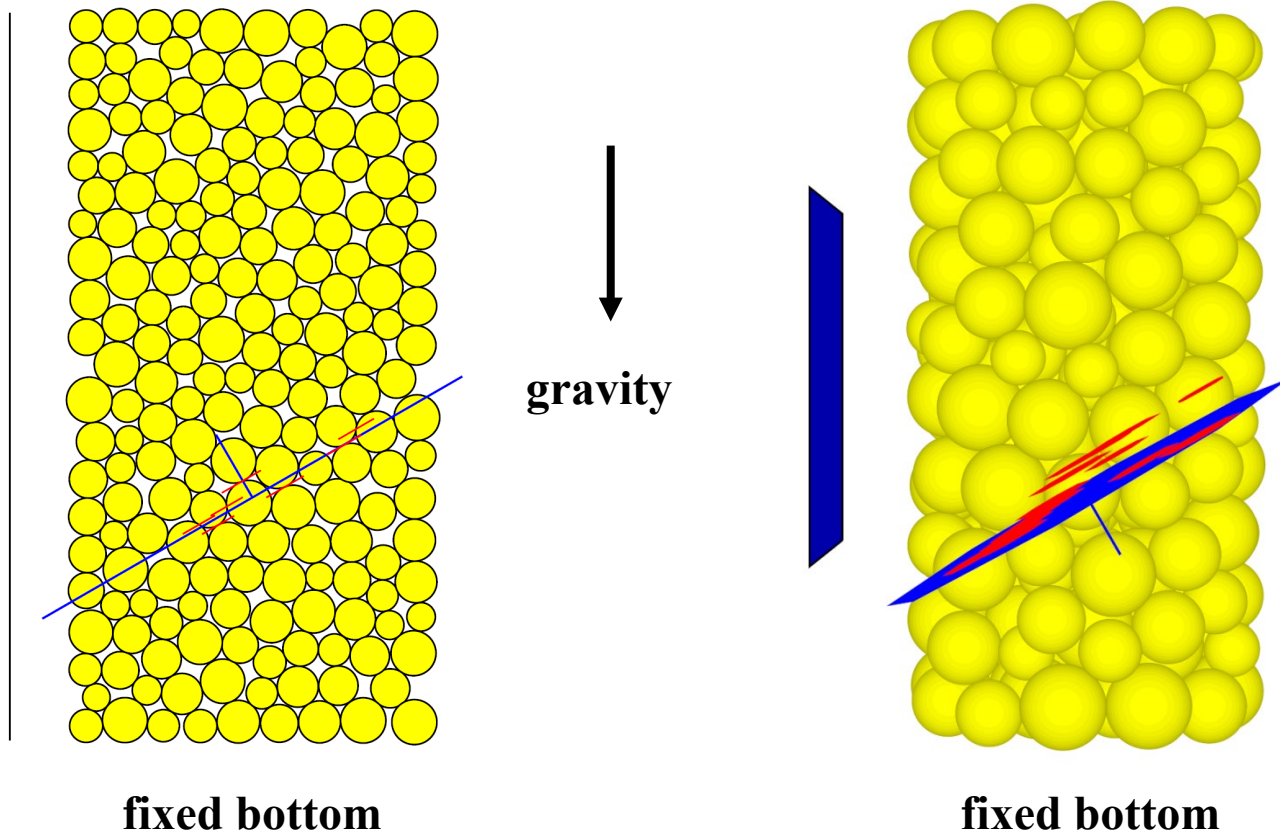
**BPM with joint**



**Joint & smooth-joint  
contacts**

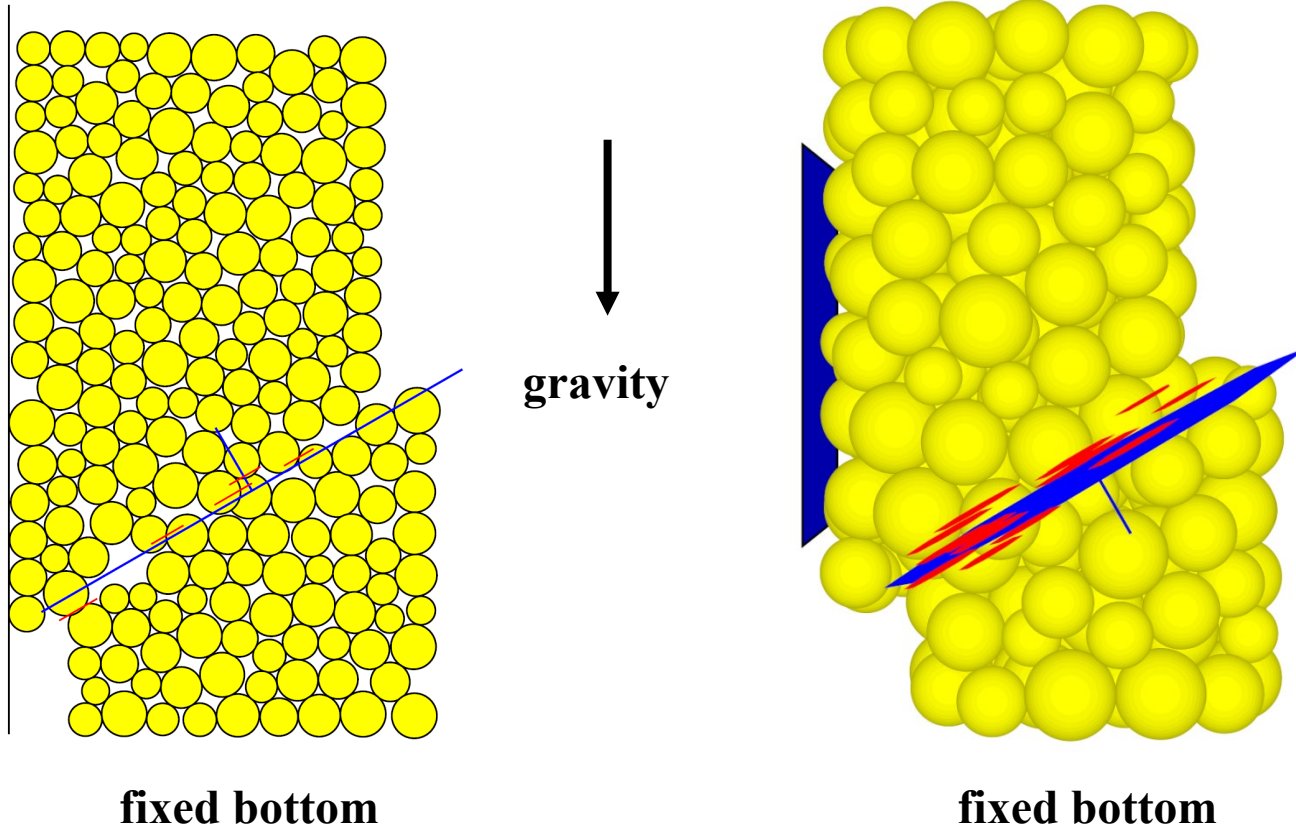
# smooth-joint contact (behavior summary)

Joint friction coefficient equals one. . .



# smooth-joint contact (behavior summary)

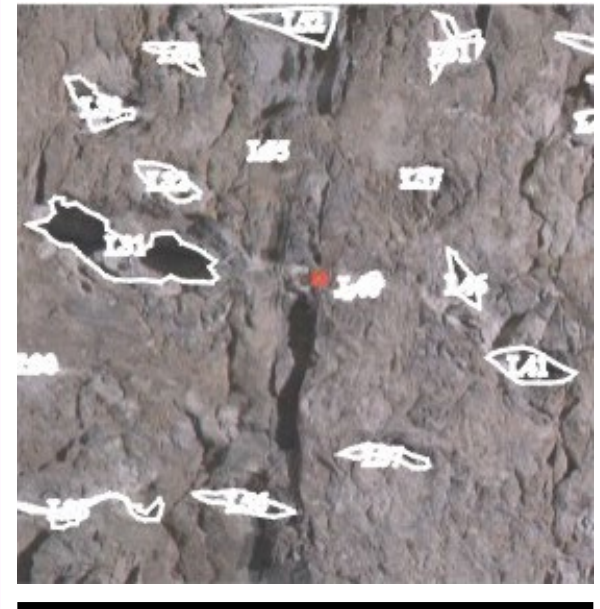
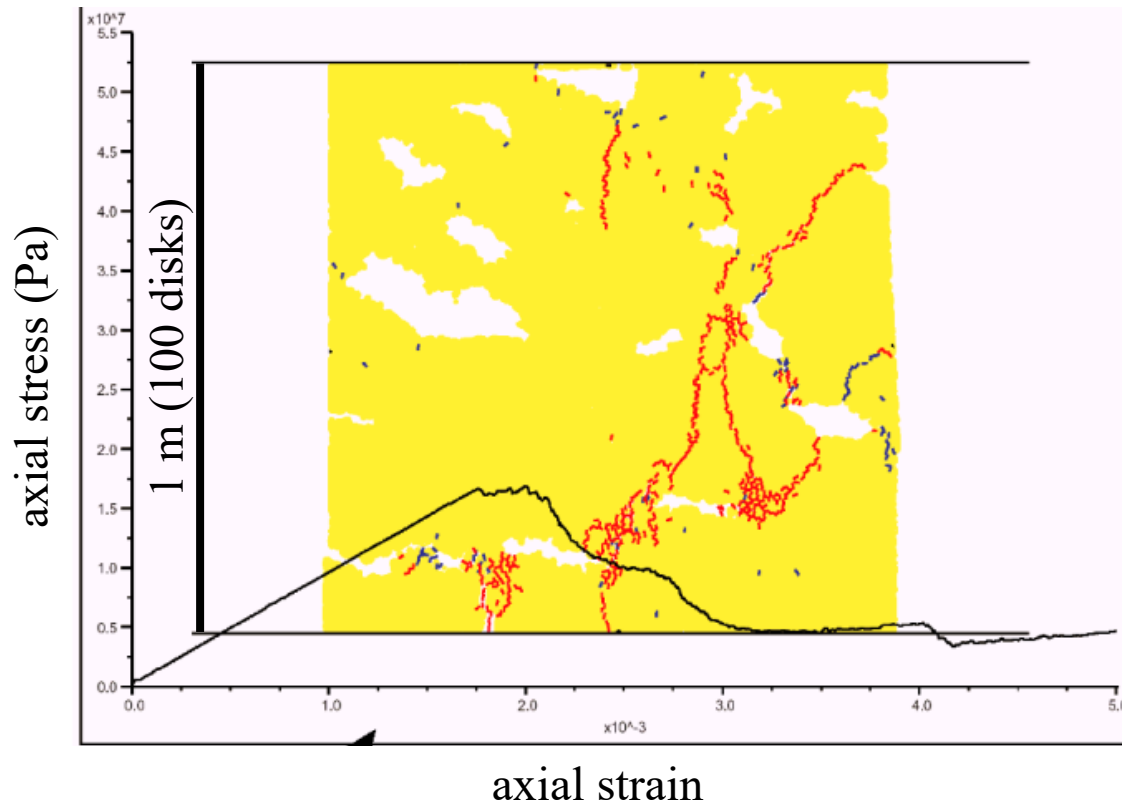
Joint friction coefficient equals zero. . .



# Microstructural Models Provided by BPM

Void regions are identified...

- grains within these regions are removed

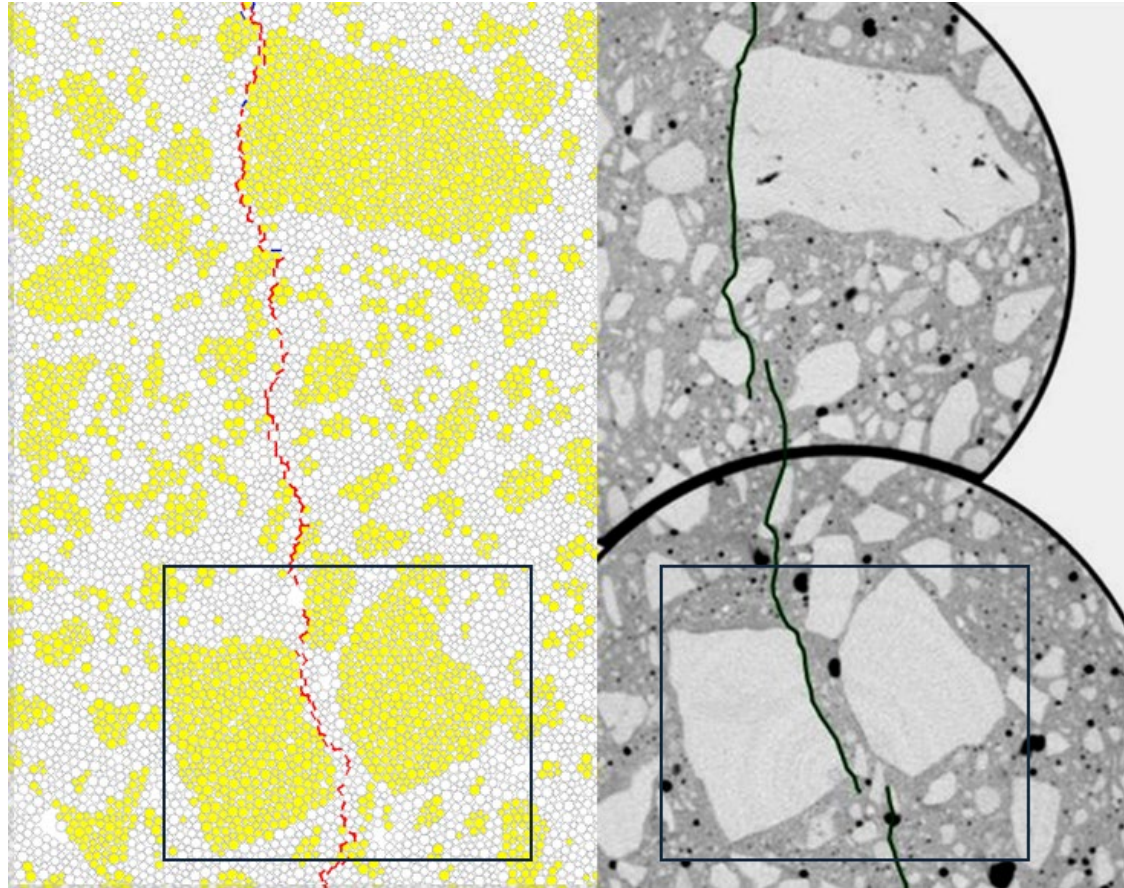


1 meter

# Microstructural Models Provided by BPM

**Material regions** are identified...

- grains & contacts within these regions are assigned properties



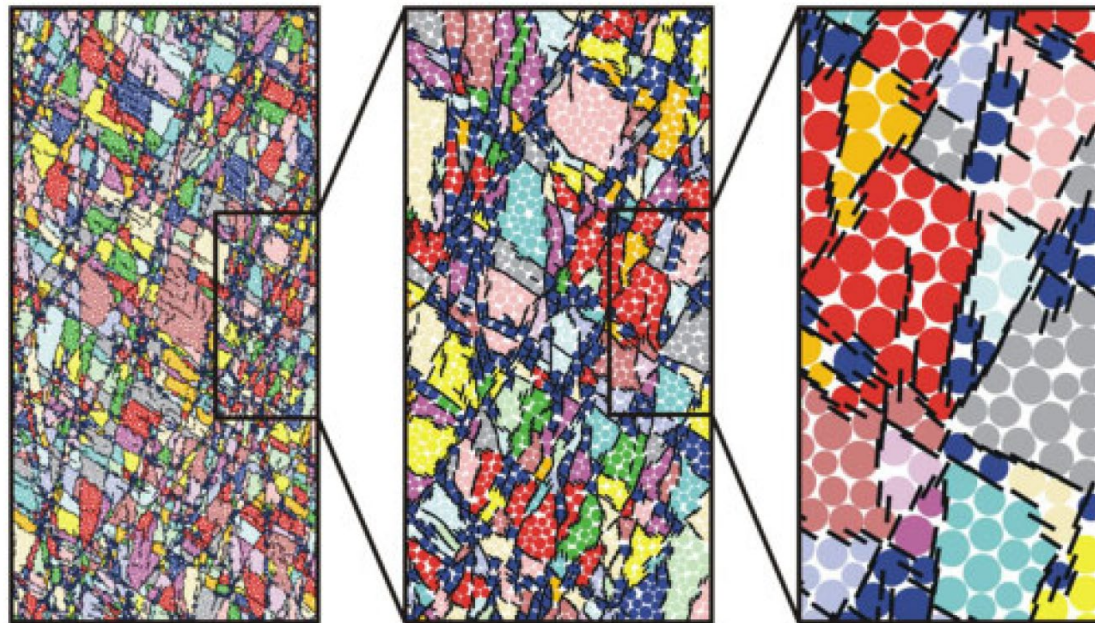
Katsaga (2010)

# Microstructural Models Provided by BPM

**Joints** are identified...

- contacts that lie along these joints are assigned properties

Synthetic Rock Mass (SRM)



SRMs are used to represent a rock mass. The BPMs are remarkably complex, and used to study impact of joint fabric on rock mass strength, brittleness and fragmentation.

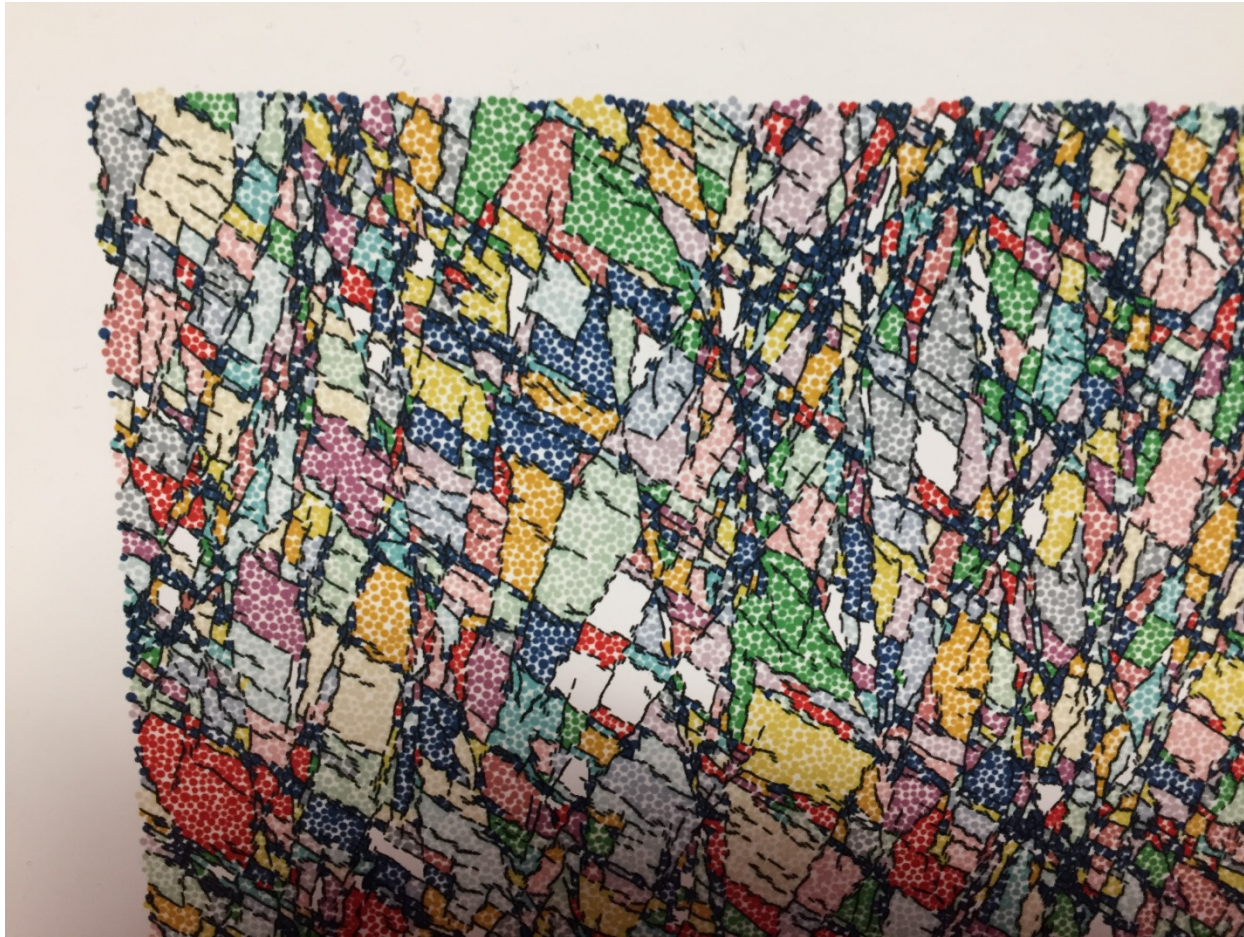
# Microstructural Models Provided by BPM

## Synthetic Rock Mass (SRM)



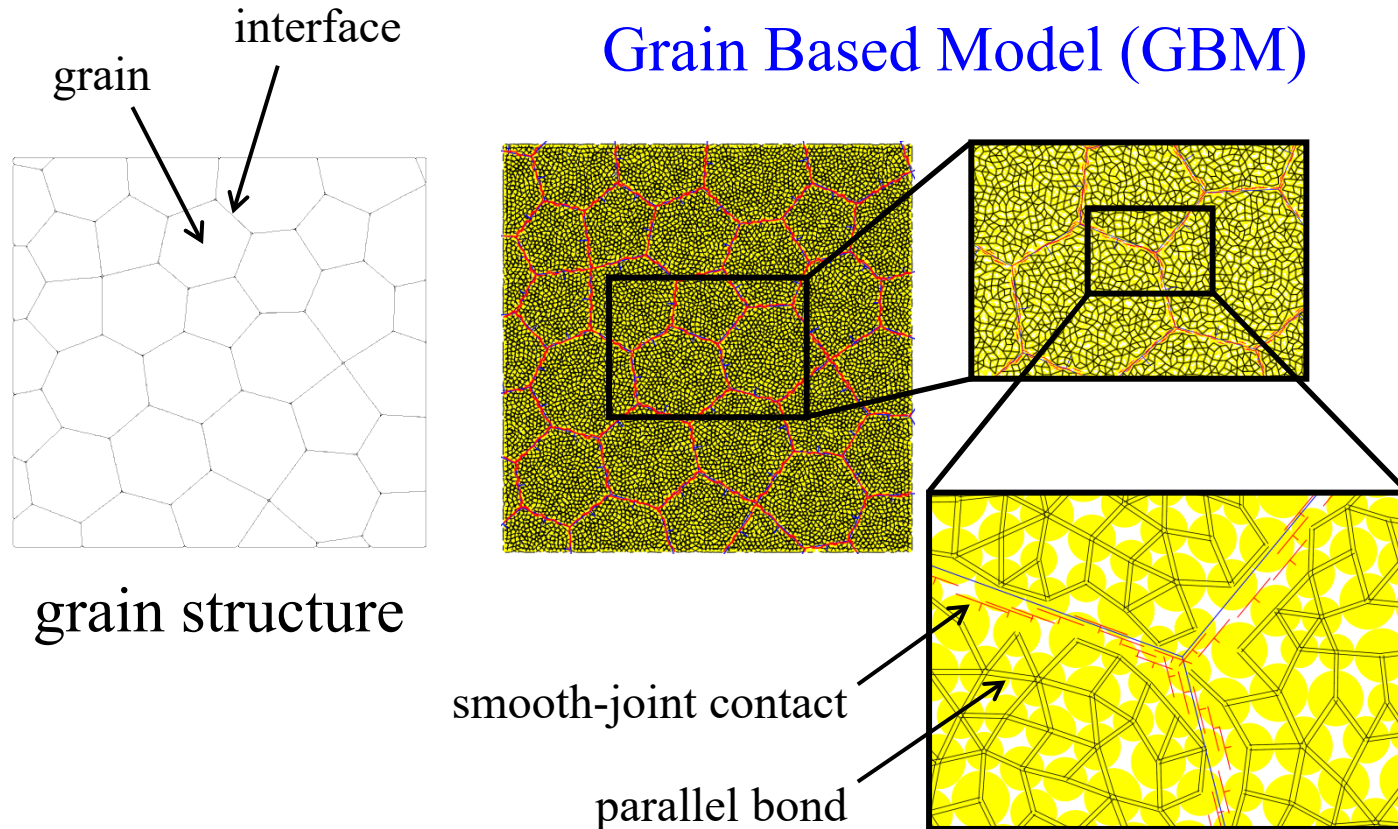
# Microstructural Models Provided by BPM

## Synthetic Rock Mass (SRM)



# Microstructural Models Provided by BPM

Material regions & joints are identified...



GBMs are used to represent intact compact rock, allow partial interface damage and grain breakage.

# Examples

Ceramic bead & Undercut cemented backfill

Matching uniaxial & tensile strengths of compact rock

- two alternative intact BPMs

Embed BPM within larger continuum model

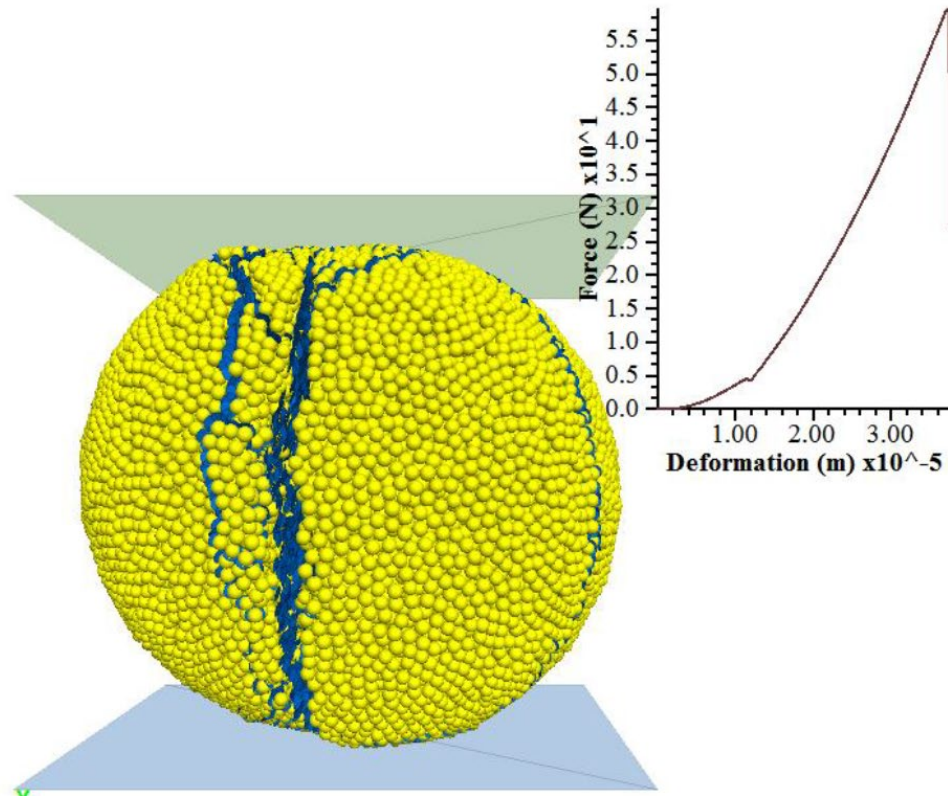
- study fracturing around advancing stope in quartzite

Sandstone Perforation Failure

# Examples (ceramic bead PFC3D, parallel-bonded material)

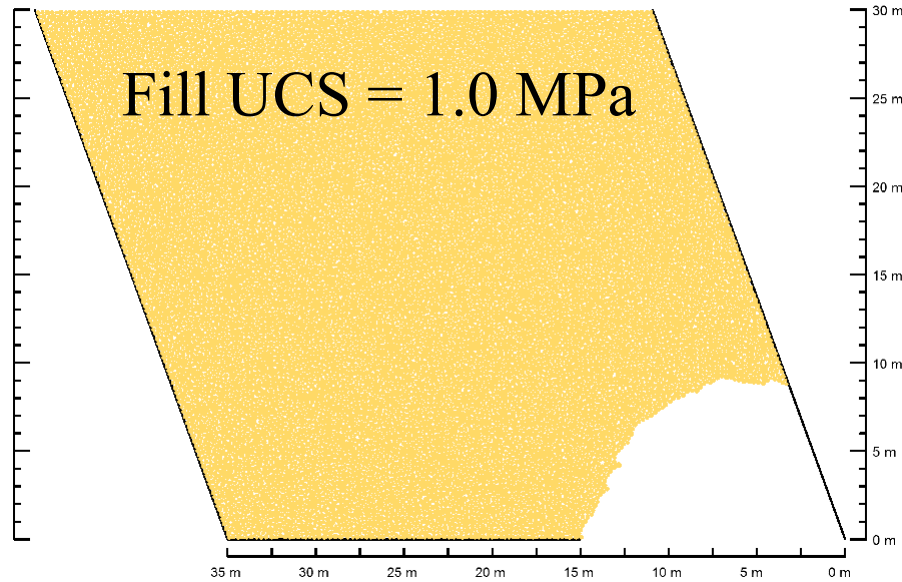
These models:

- \* Matched Hertzian response
- \* Computed breakage stress (solid & hollow beads)

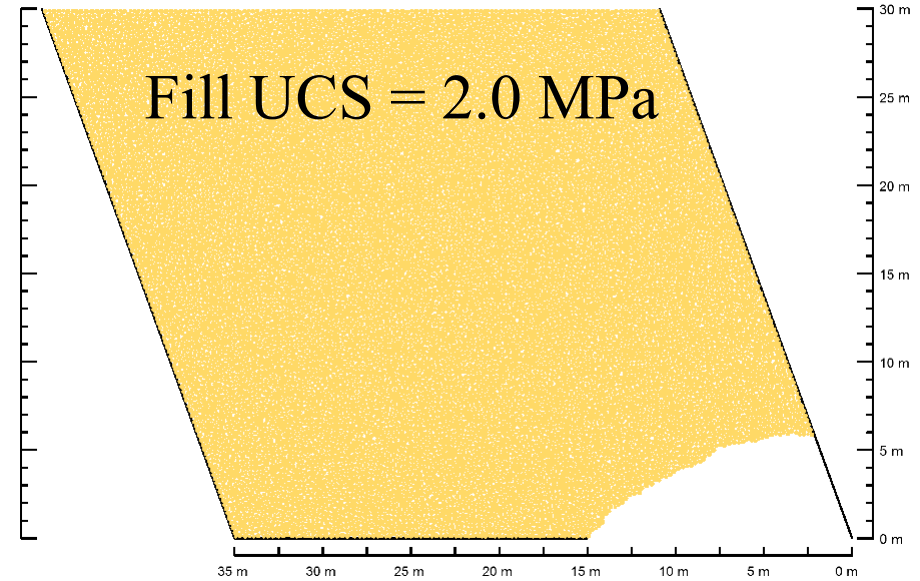


# Examples (undercut cemented backfill PFC2D, flat-jointed material)

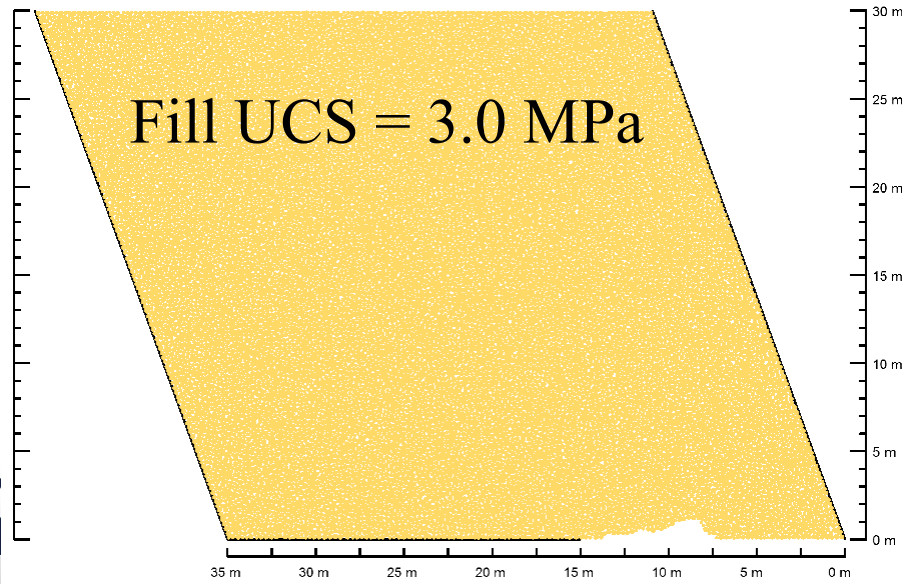
Fill UCS = 1.0 MPa, Panel = 15.0 m



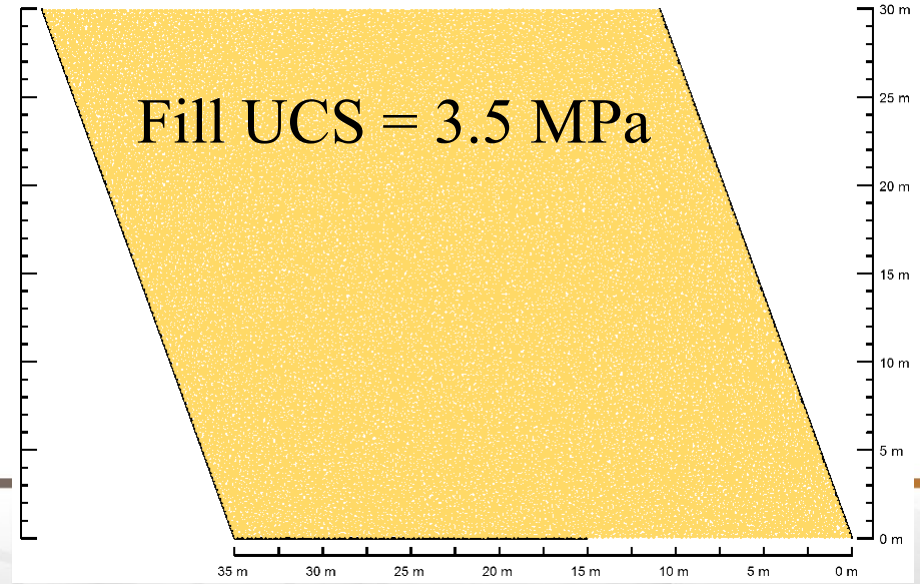
Fill UCS = 2.0 MPa, Panel = 15.0 m



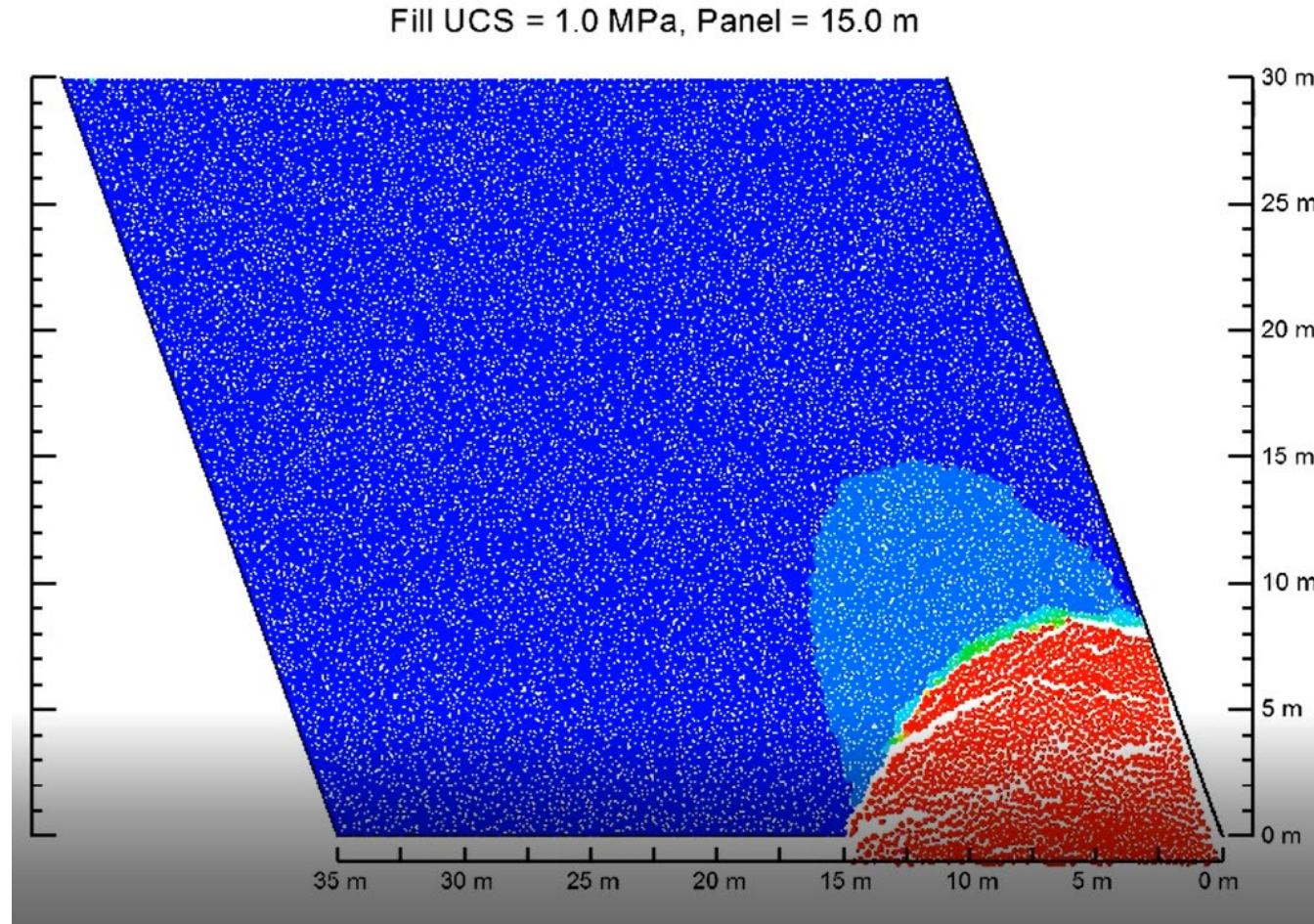
Fill UCS = 3.0 MPa, Panel = 15.0 m



Fill UCS = 3.5 MPa, Panel = 15.0 m



# Examples (undercut cemented backfill PFC2D, flat-jointed material)



# Examples

Ceramic bead & Undercut cemented backfill

Matching uniaxial & tensile strengths of compact rock

- two alternative intact BPMs

Embed BPM within larger continuum model

- study fracturing around advancing stope in quartzite

Sandstone Perforation Failure

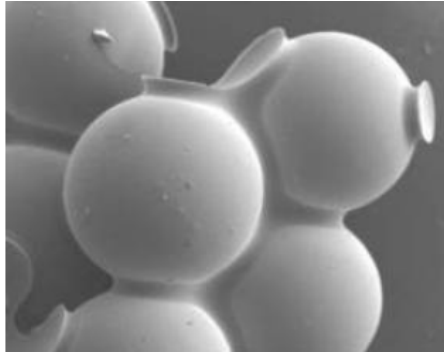
# Examples (match uniaxial & tensile strengths)

BPM of parallel-bonded disks or spheres cannot match both tensile and compressive strengths of typical compact rock.

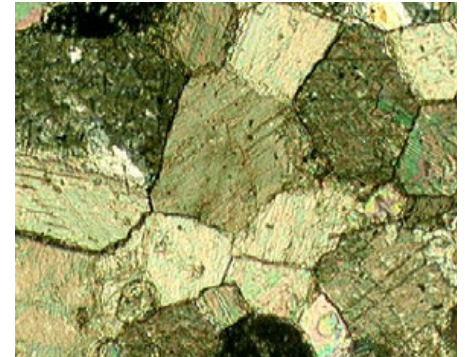
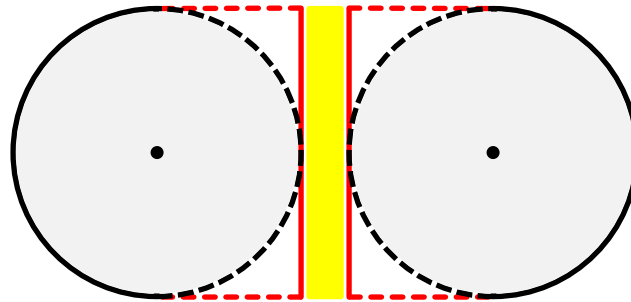
This limitation is overcome by introducing intergranular interlock in the form of a well-connected grain structure with interfaces that are deformable, breakable and can sustain partial damage.

Partial interface damage with continued moment-resisting ability is an important microstructural feature of a BPM.

# Flat-jointed material (Differs from parallel bond)

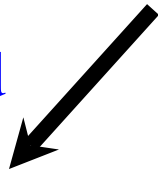


intact parallel bond

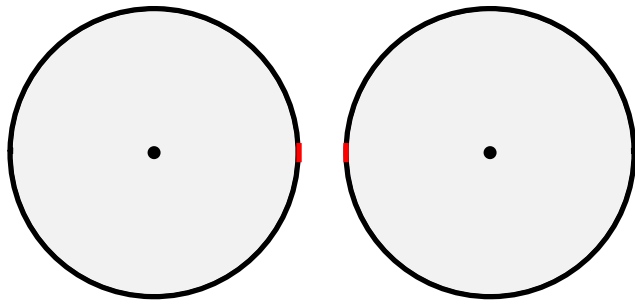
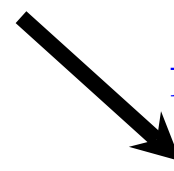


bonded finite-length interface

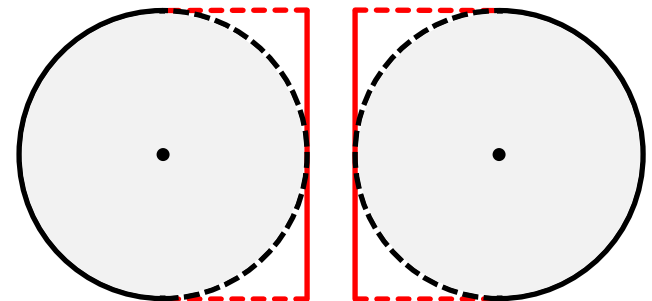
broken parallel bond



fully broken flat joint



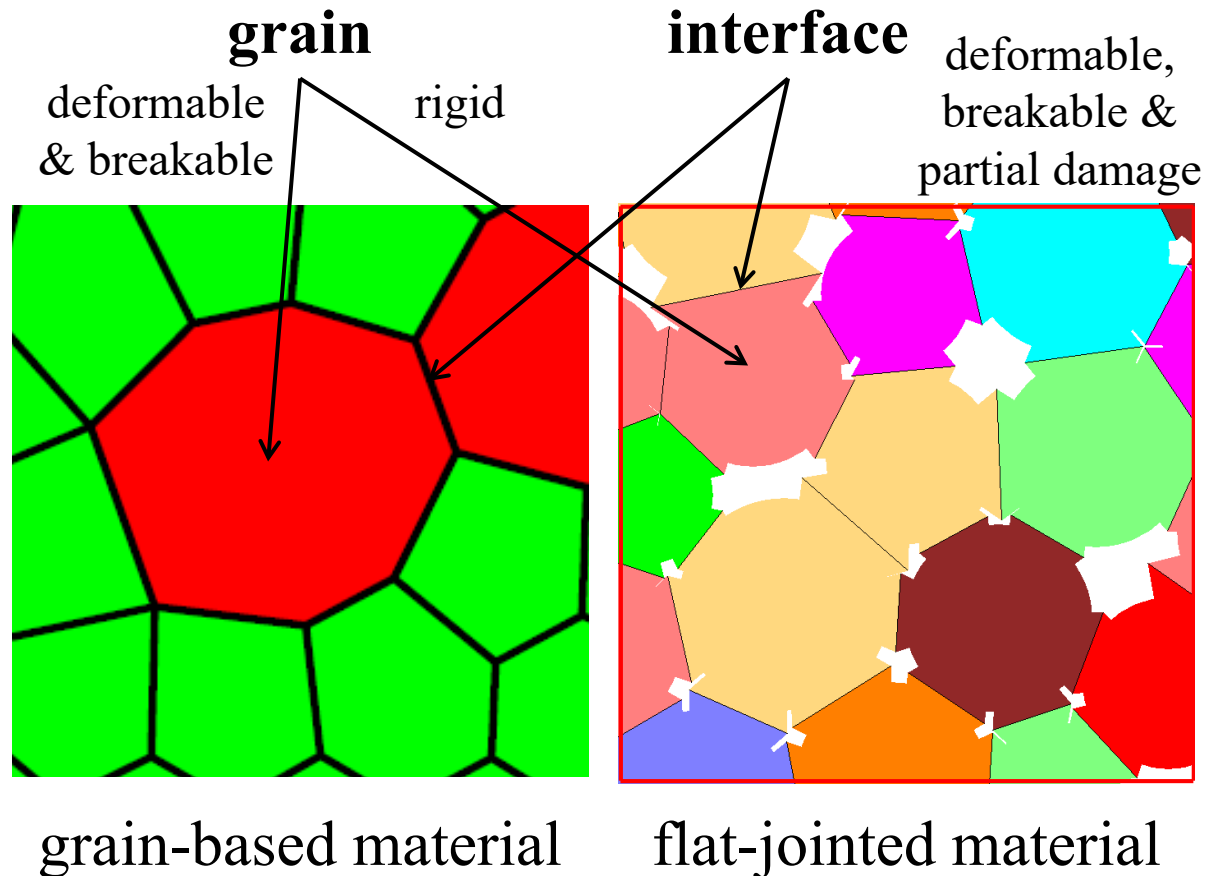
frictional zero-length interface



frictional finite-length interface

# Examples (match uniaxial & tensile strengths)

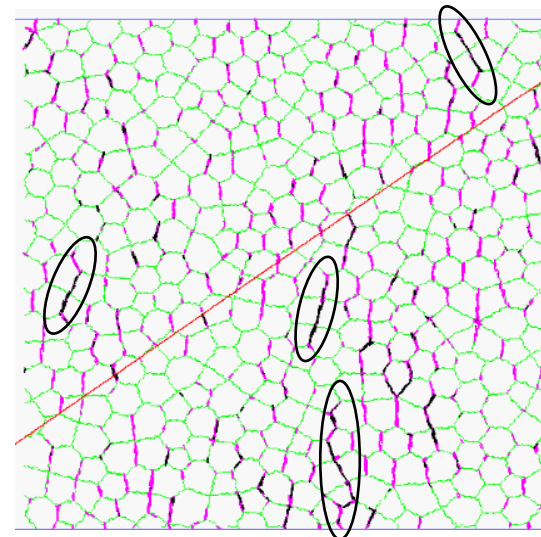
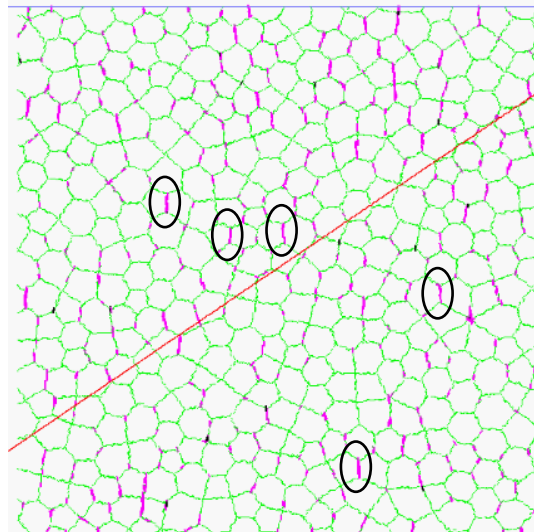
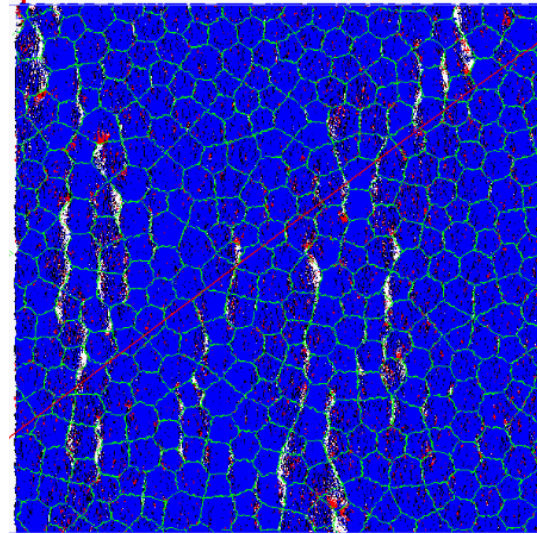
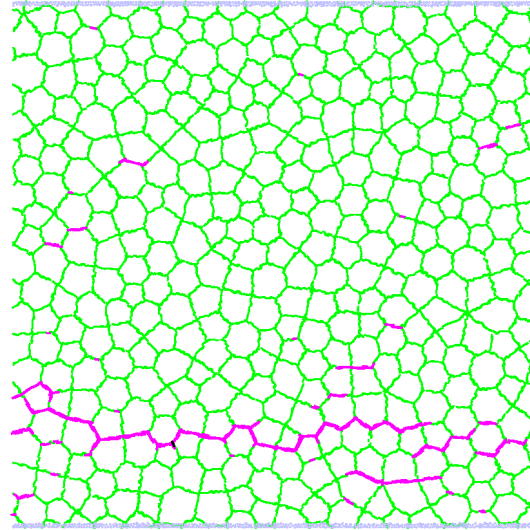
Two alternative intact BPMs:



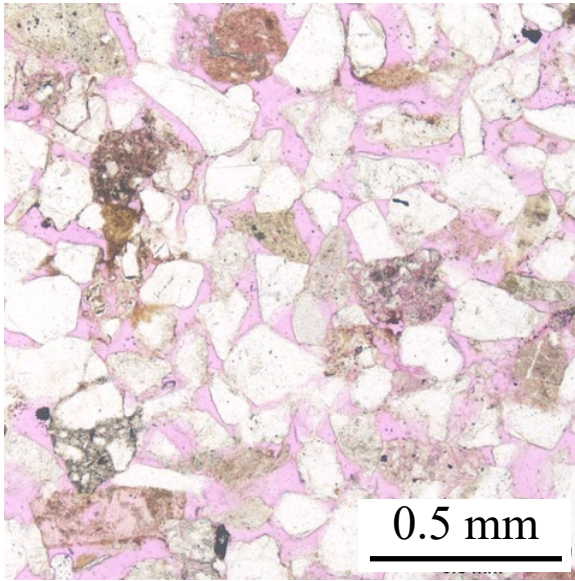
# Examples (grain-based material)

*axial splitting*

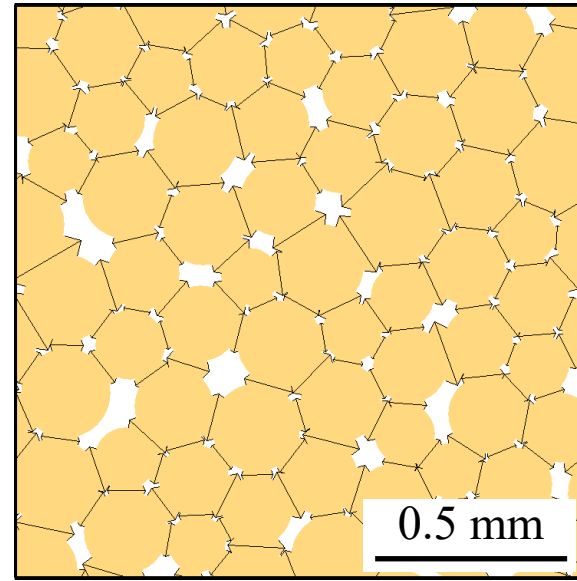
50 mm (200 disks, 20 grains)



# Examples (flat-jointed material)



Castlegate sandstone

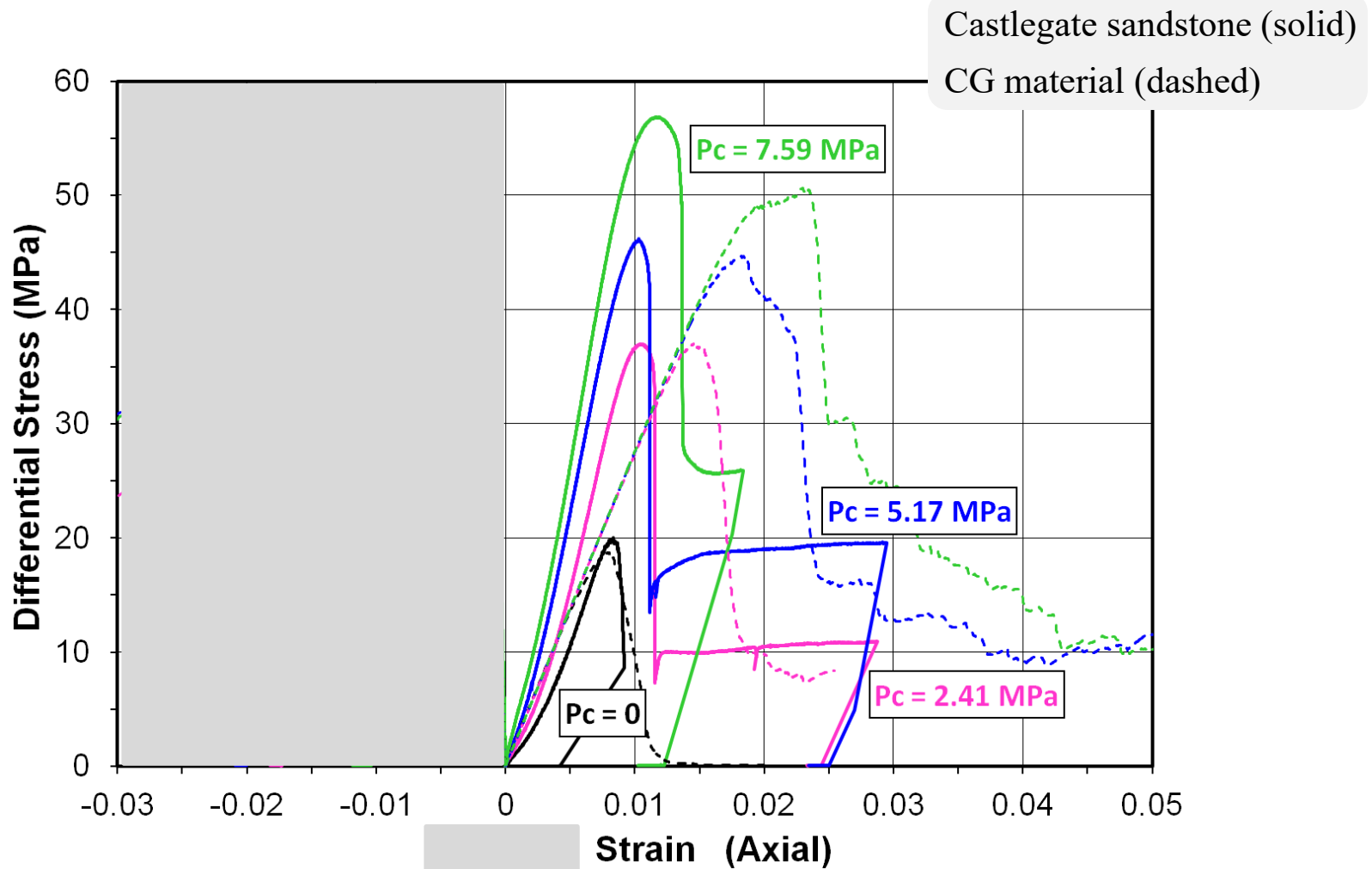


CG material

Potyondy, D.O. (2017) "Simulating Perforation Damage with a Flat-Jointed Bonded-Particle Material," paper ARMA 17-223 in Proceedings of 51st U.S. Rock Mechanics/Geomechanics Symposium, San Francisco, USA, 25–28 June 2017. [2D flat-jointed sandstone material --- described here.]

Potyondy, D.O. (2018) "A Flat-Jointed Bonded-Particle Model for Rock," paper ARMA 18-1208 in Proceedings of 52nd U.S. Rock Mechanics/Geomechanics Symposium, Seattle, USA, 17–20 June 2018. [3D flat-jointed granite material]

# Material Behavior (compression tests)



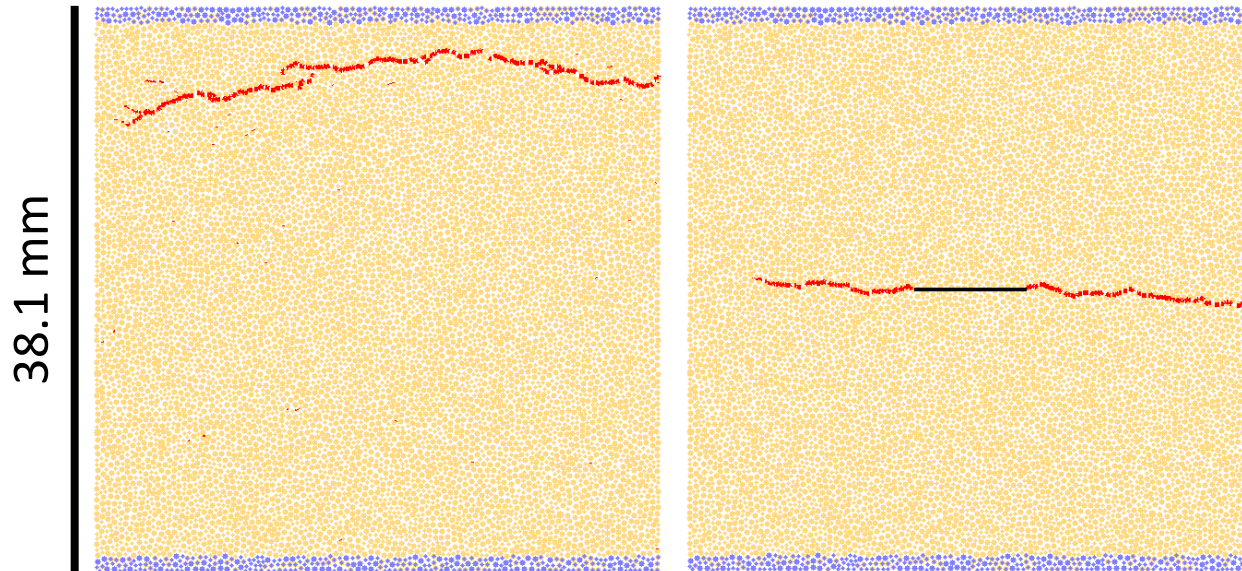
Stress-strain response during triaxial testing

# Material Behavior (tension & compression tests)

- The mechanisms that are exhibited during tension & compression tests are like the brittle failure behavior of compact rock, with the exception that transgranular cracking occurring within and across grains during compression tests is absent.
- The following mechanisms are exhibited during these tests and shown on the next 5 slides.

# Direct-tension (& fracture-toughness) tests

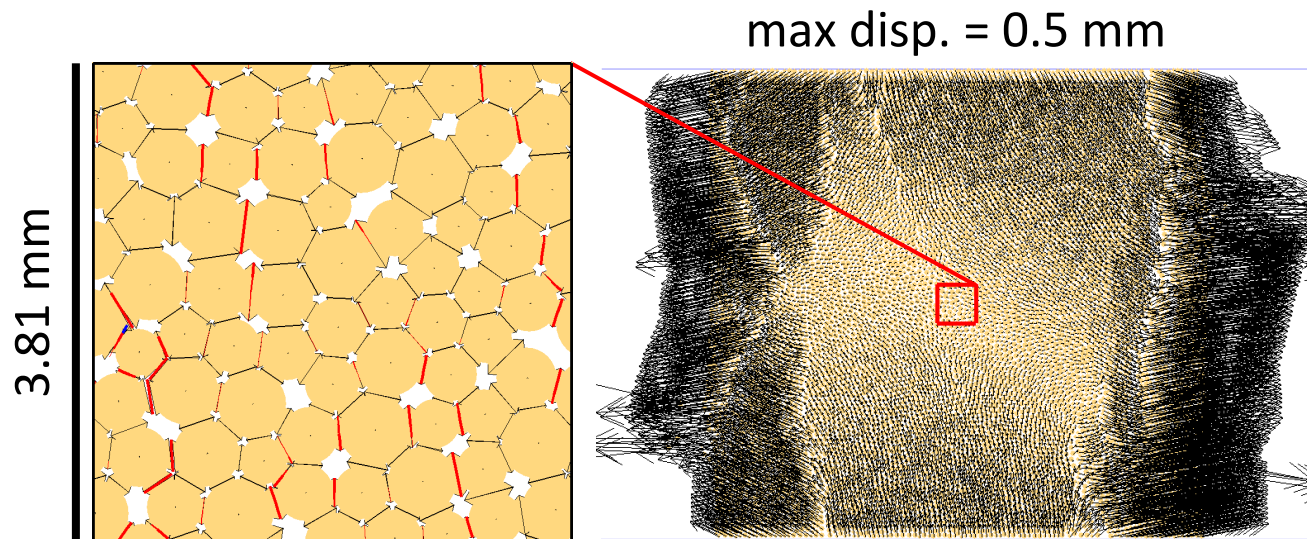
- Peak stress coincides with formation of a few tensile fractures aligned perpendicular to specimen axis.



Damaged microstructure at post-peak state of tension tests.

# Compression test (unconfined)

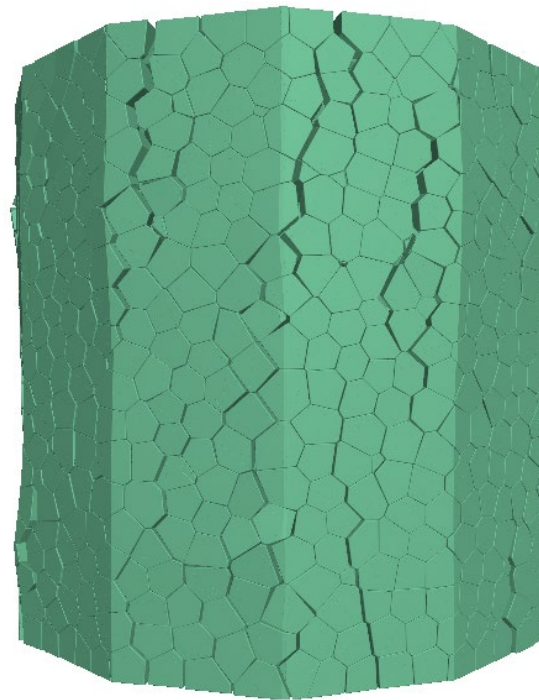
- Peak stress coincides with axial splitting in which the material breaks apart into multiple interlocking columns.



Damaged microstructure at post-peak state of UCS test.

# Compression test (unconfined)

- Peak stress coincides with axial splitting in which the material breaks apart into multiple interlocking columns.

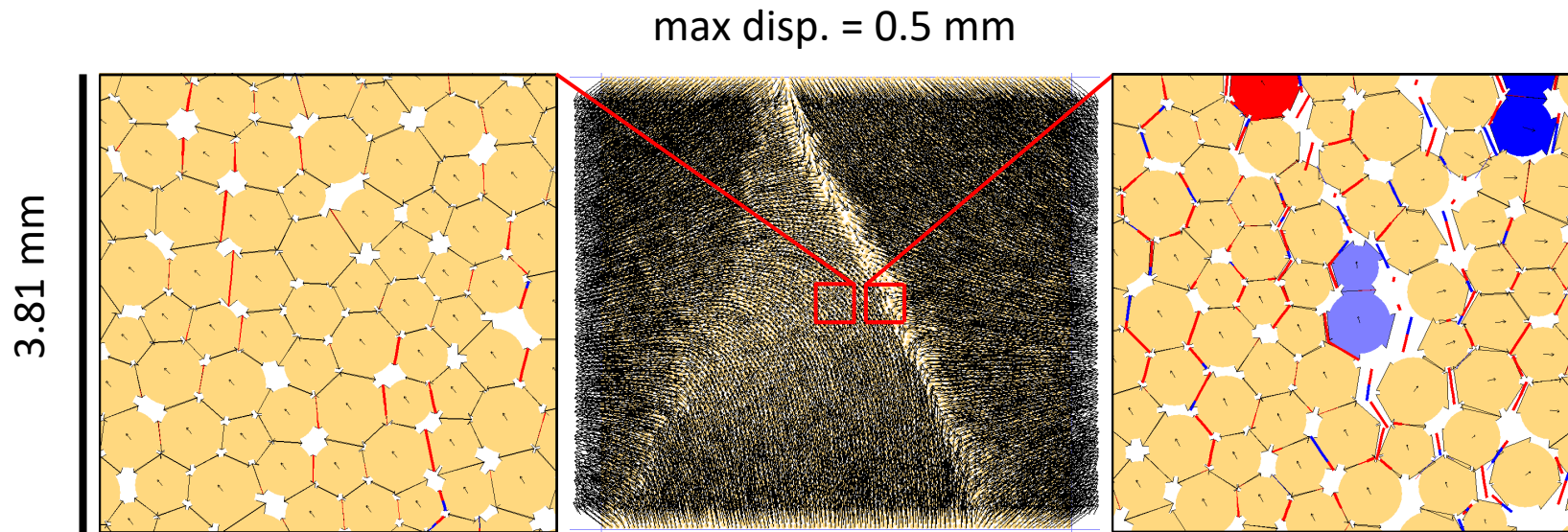


**bonded  
Voronoi grains**

Damaged microstructure at post-peak state of UCS test.

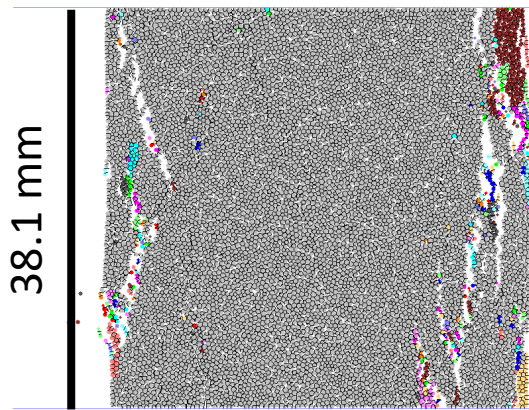
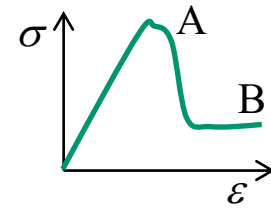
# Compression test (confined)

- Peak stress coincides with formation of a few diagonally aligned shear fractures.

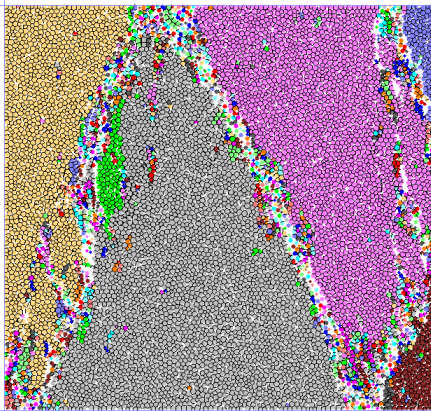
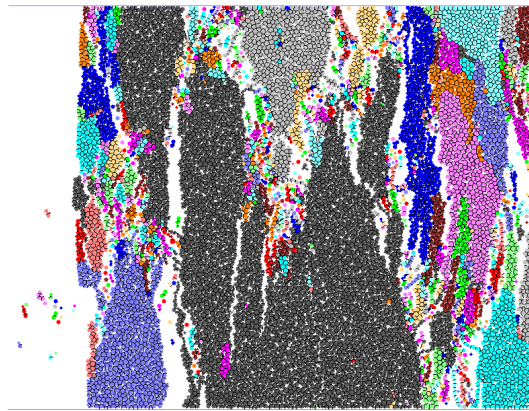


Damaged microstructure at post-peak state of confined-compression test.

# Compression tests (fragmentation)



post-peak (A)



residual (B)

$P_c = 0$

$P_c = 2.41 \text{ MPa}$

Fragmentation at post-peak (top) and residual (bottom) states of compression tests.

# Examples

Ceramic bead & Undercut cemented backfill

Matching uniaxial & tensile strengths of compact rock

- two alternative intact BPMs

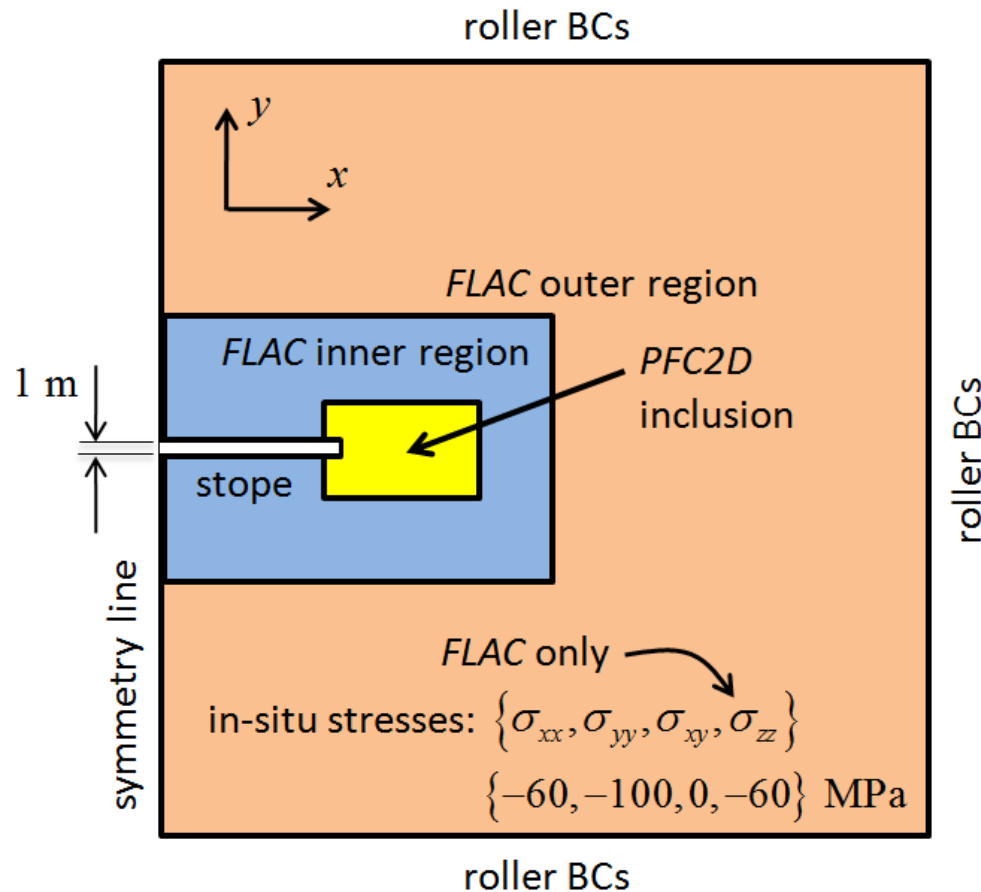
Embed BPM within larger continuum model

- study fracturing around advancing stope in quartzite

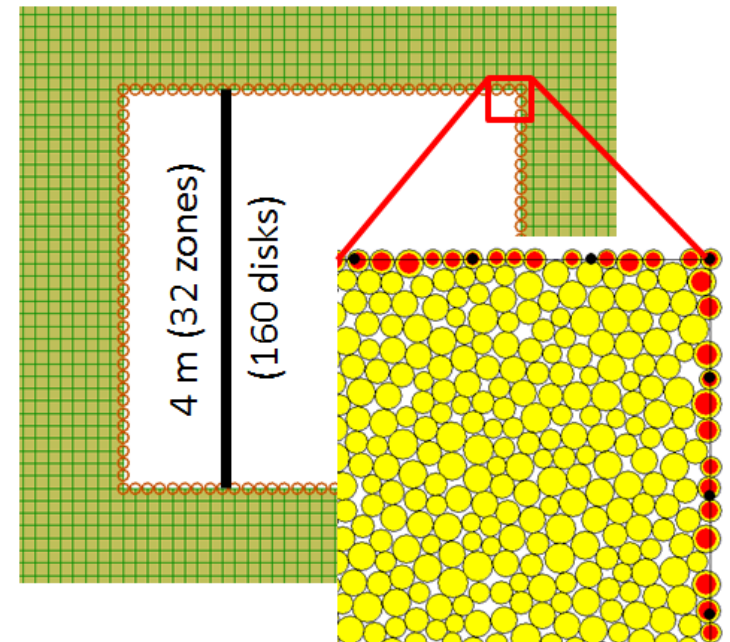
Sandstone Perforation Failure

# Examples (embed BPM in continuum model)

**quartzite** modeled (continuum) as strain-hardening/softening material  
*ad hoc* strength reduction (intact → in-situ)



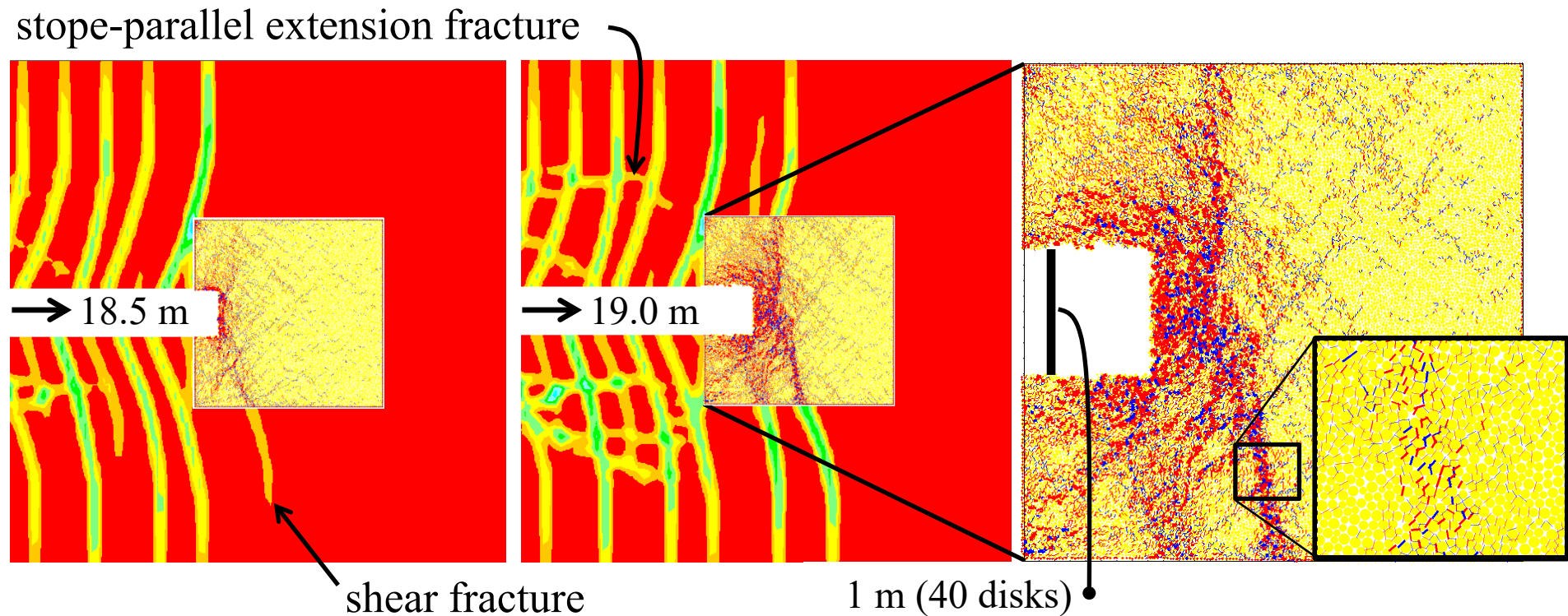
**Coupled model**



**PFC2D inclusion**

# Examples (embed BPM in continuum model)

Fracture pattern compares well with expected pattern.



Could benefit by comparing responses of these two different material idealizations (e.g., damage processes in shear fractures).

# Examples

Ceramic bead & Undercut cemented backfill

Matching uniaxial & tensile strengths of compact rock

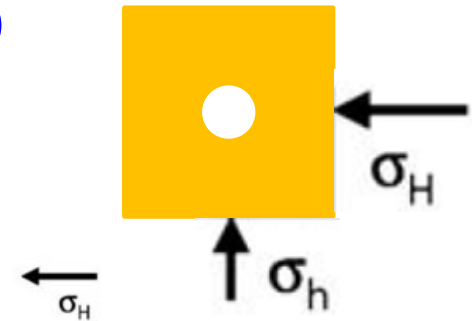
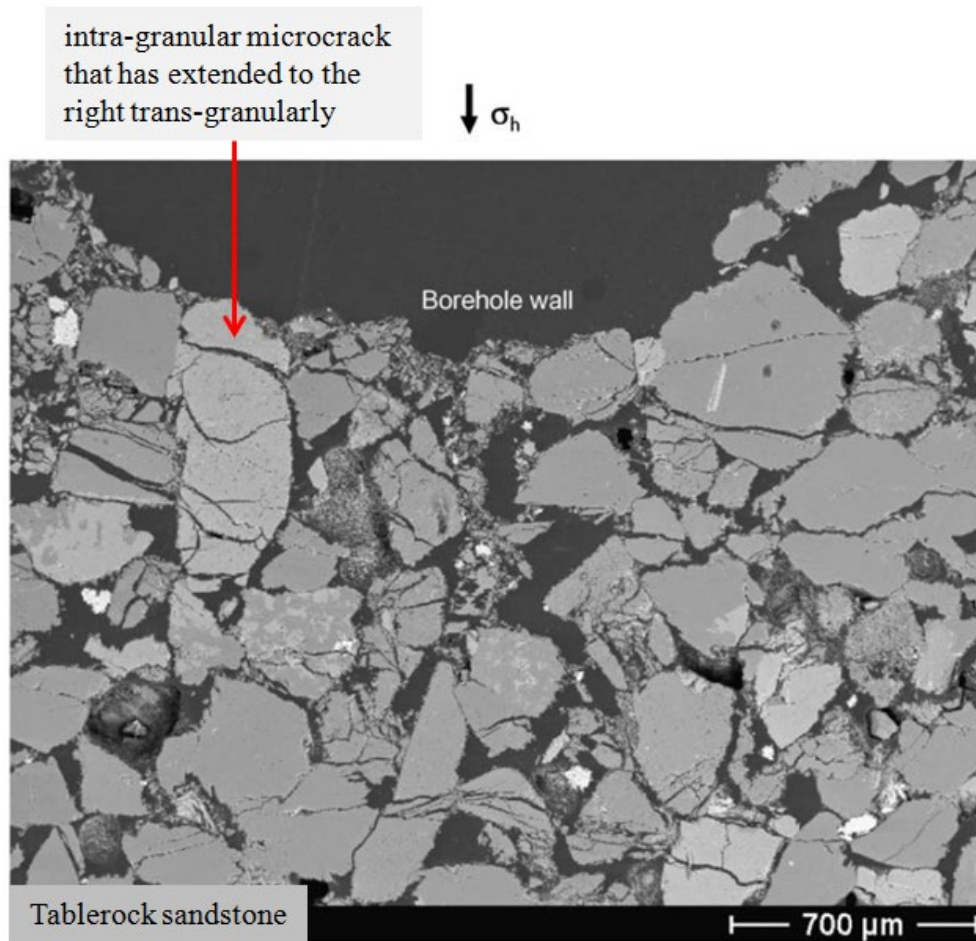
- two alternative intact BPMs

Embed BPM within larger continuum model

- study fracturing around advancing stope in quartzite

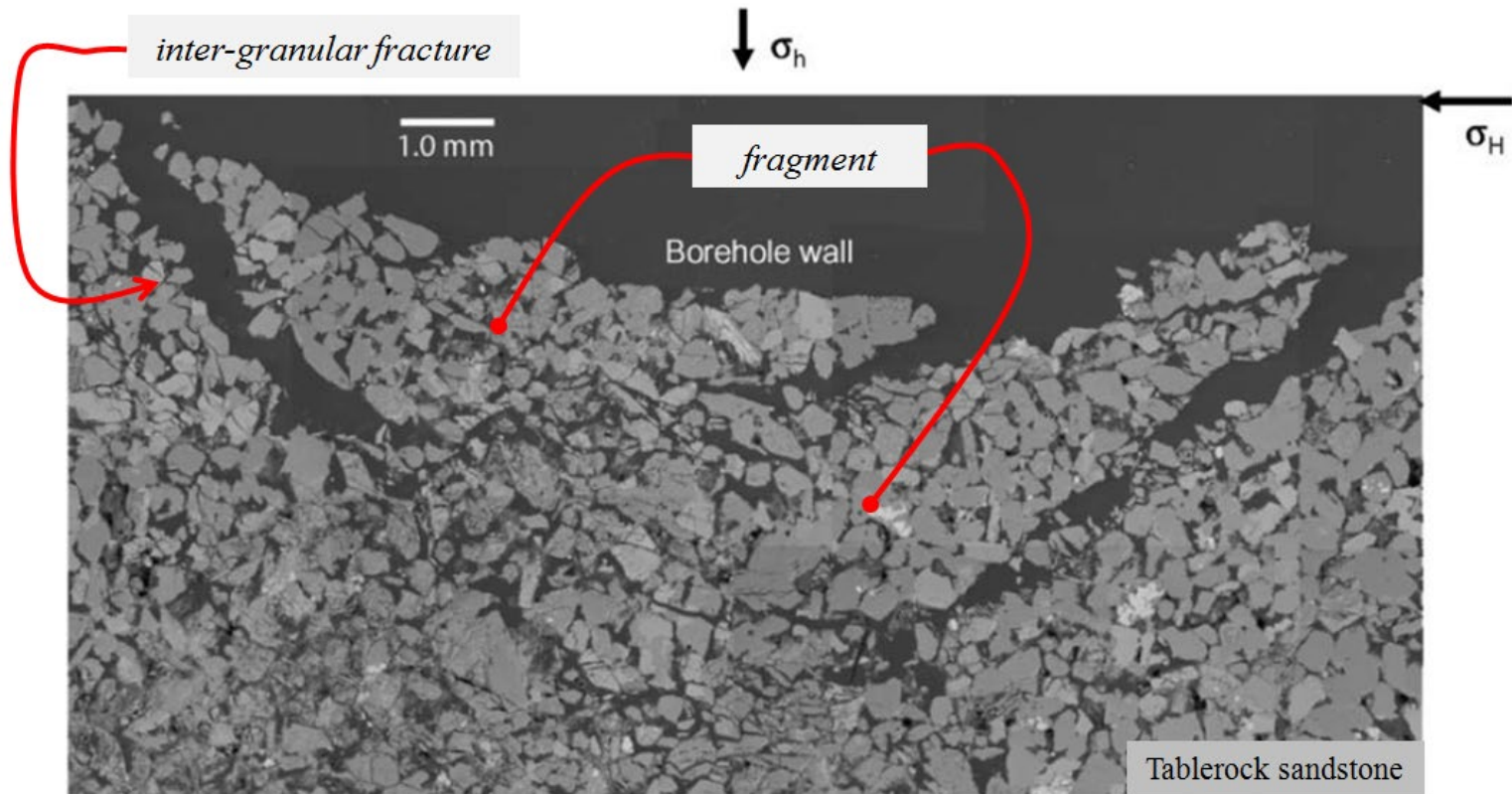
Sandstone Perforation Failure

# Examples (sandstone perforation failure)



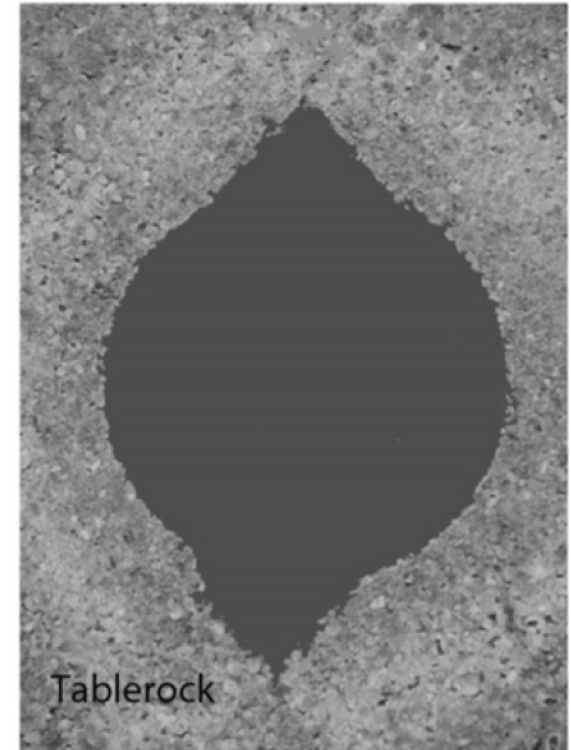
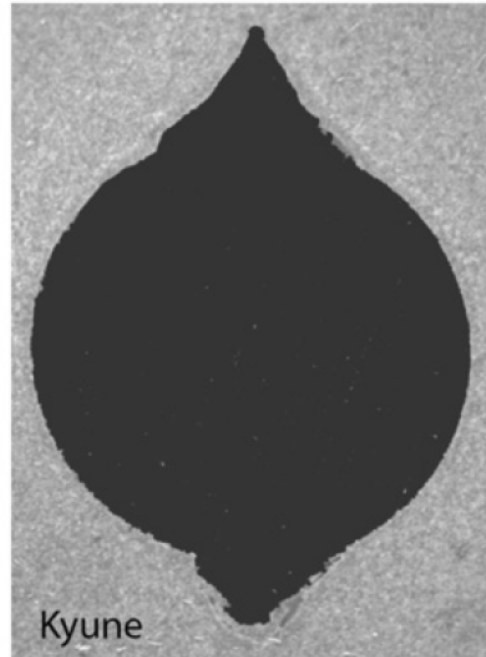
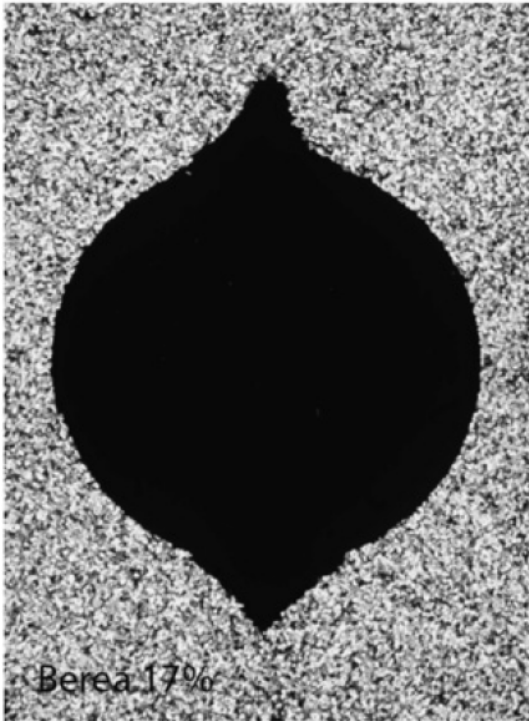
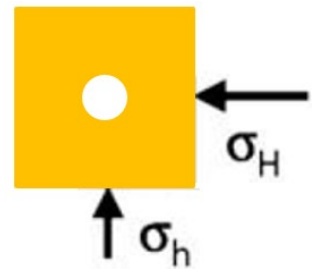
Damage begins as swarm of intra-granular microcracks, that first extend transgranularly, loosening grains and grain fragments...

# Examples (sandstone perforation failure)



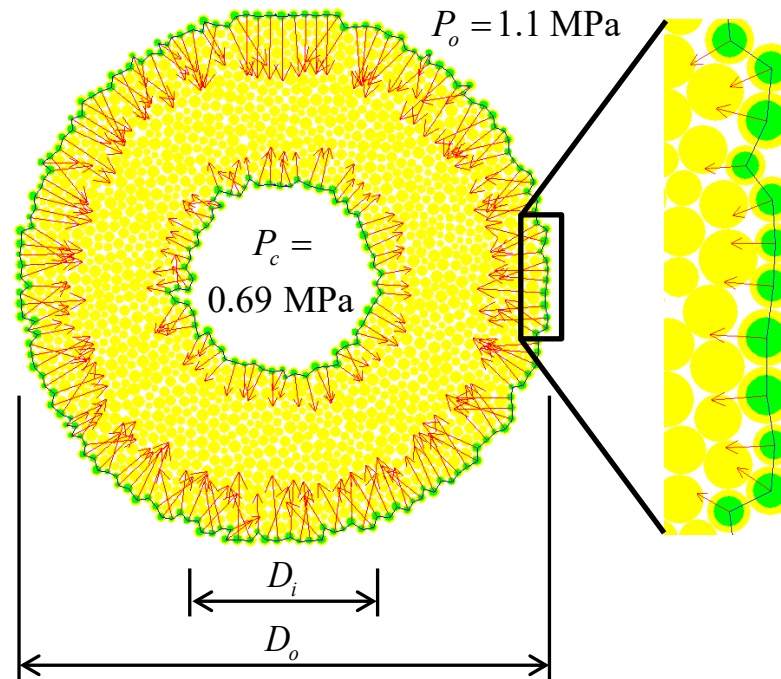
...and then extend inter-granularly toward borehole wall, where a thin layer of grains & fragments begins to separate (ready to spall or be removed by drilling fluid).

# Examples (sandstone perforation failure)



This episodic process produces wide-angle, dog-eared breakouts.

# Examples (sandstone perforation failure)



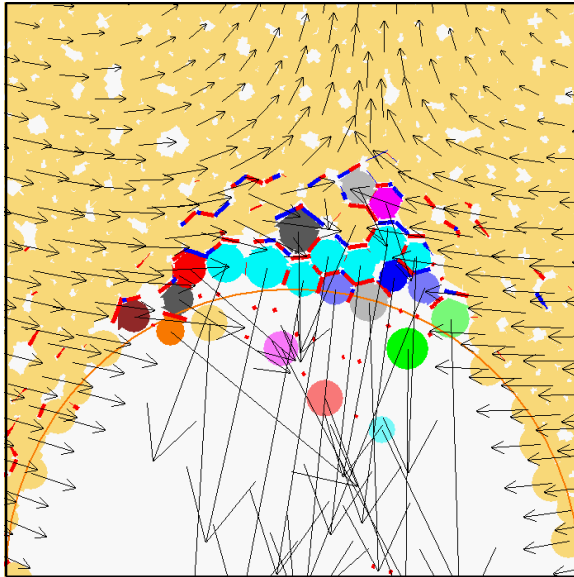
Model of a Thick-Walled Cylinder test  
showing pressure-application procedure

# Examples (sandstone perforation failure)

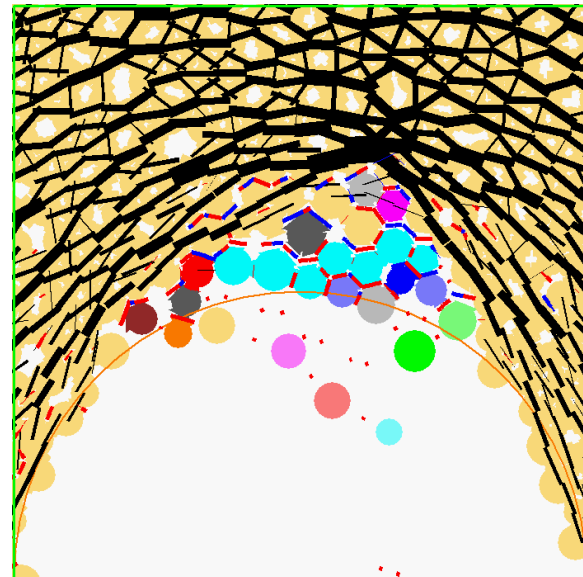
We now describe the formation of a stable notch above the borehole when the external pressure reaches 30.5 MPa.

■ damage

■ damage & forces



$P_o = 30.5$  MPa (stable)

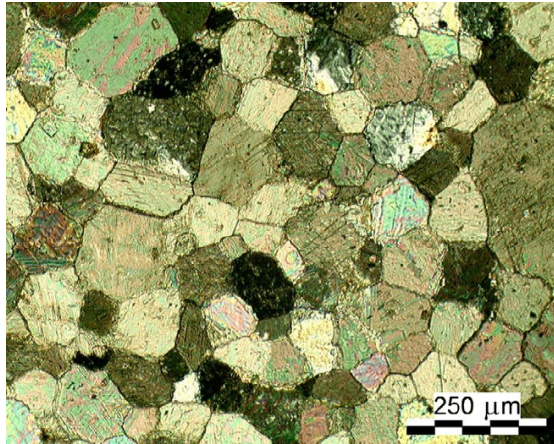


$P_o = 30.5$  MPa (stable)

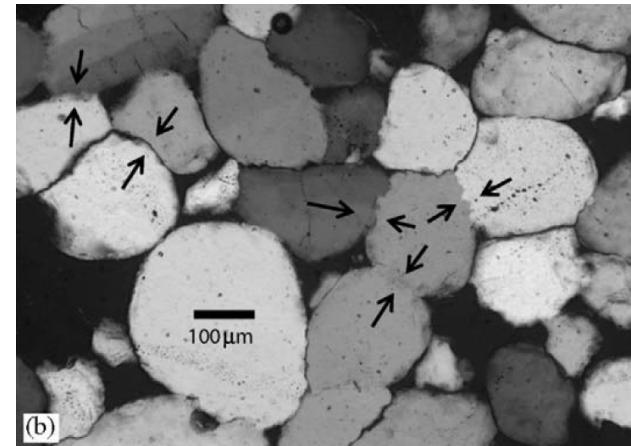
# Conclusions & Future Directions

Bonded-particle modeling is in early phase of development

- have generic models for 2D & 3D intact compact rock
- Next step: generic model of intact porous rock



marble with interlocking grains



Haimson (2007)

sandstone with broad grain sutures

# Conclusions & Future Directions

All BPM modeling benefits from increased computational speed via

- multi-threading capability in *PFC2D* and *PFC3D* 5.0 & above!
- support for MPI under development

# Conclusions & Future Directions

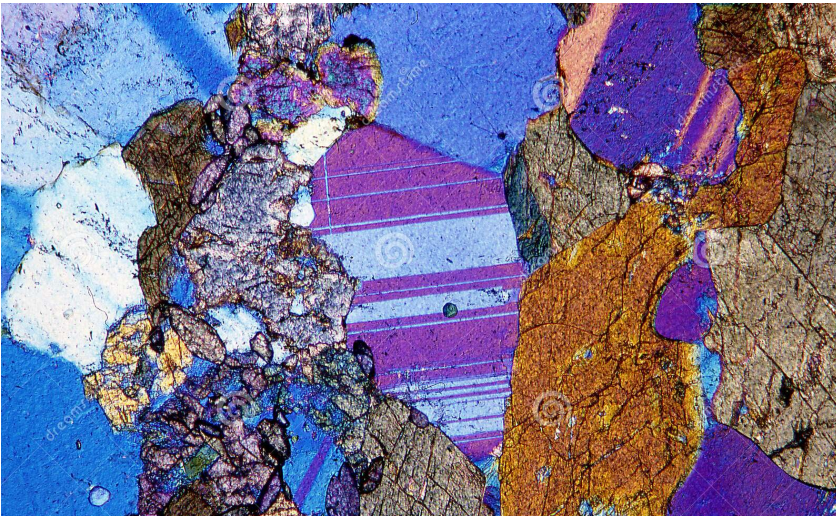
With continuing increases in computational speed, BPM modeling will be increasingly applied to boundary-value problems

- How to incorporate scale effects that make in-situ strength less than intact strength?

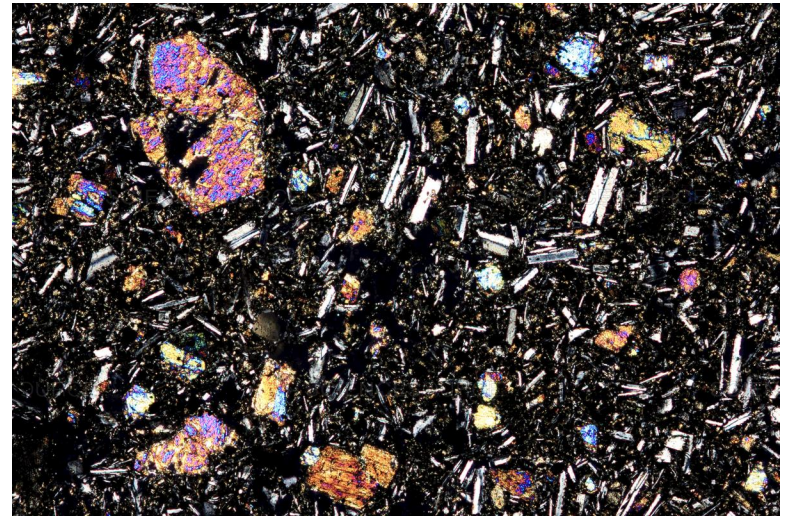
# Conclusions & Future Directions

Future BPMs should be constructed to match particular types of rock

- granite, sandstone, limestone,...



Granite  
(minerals)



Basalt  
(minerals & matrix)

# Conclusions & Future Directions

Challenge is to keep models as simple as possible

- include features to allow relevant micromechanisms to occur

Closer match to microstructural & structural features →

Closer match to macroscopic behavior